

# ハイブリッド分子動力学計算によるプロテイン・スプライシング の反応機構の解析

Hybrid molecular dynamics simulations of catalytic reaction  
of protein splicing

(Project in progress. Started: Jan. 2008)

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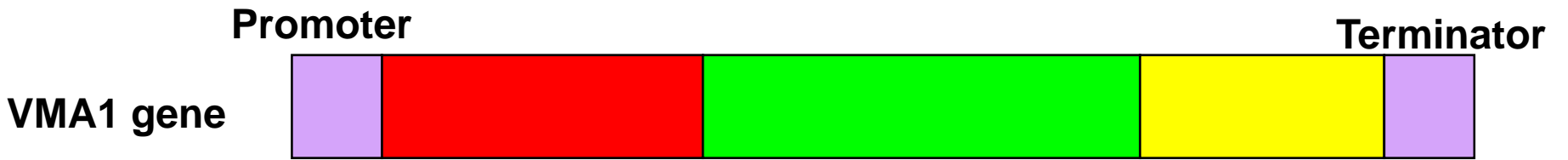
BOERO Mauro (筑波大学計算科学研究センター)

舘野 賢 (筑波大学計算科学研究センター)



# Outline of the problem

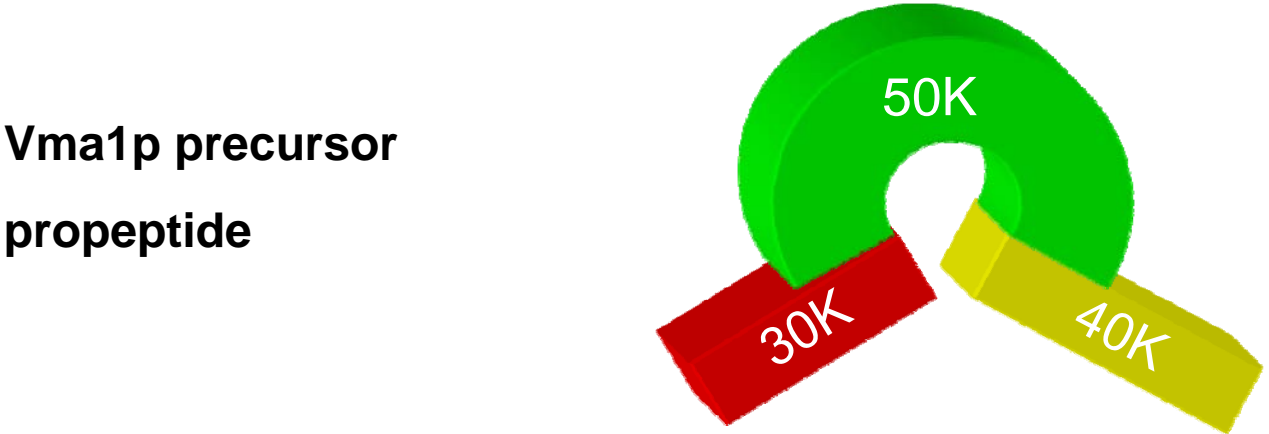
- Splicing of proteins is a common process in any bio-system, *but* it occurs so rapidly that the precursor protein is rarely observed in native systems (R. Mizutani et al. *J. Mol. Biol.* **316**, 919 (2002)).
- The process is a **fundamental reaction in of the cell**, but due to its complexity, **still largely unknown**.
- At least four nucleophilic attacks by three different residues are involved (F. B. Perler, *Nucleic Acids Res.* **30**, 383 (2002)) and a microscopic picture is hard to obtain experimentally.
- The current knowledge of the splicing mechanism comes mostly from the work of Perler (M. Q. Xu and F. B. Perler, *EMBO J.* **15**, 5146 (1996); F. B. Perler, *Nature Struct. Biol.* **5**, 249 (1998); *Cell* **92**, 1 (1998)) and Paulus (H. Paulus, *Chem. Soc. Rev.* **27**, 375 (1998))



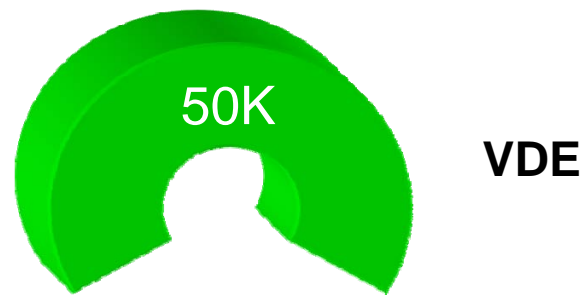
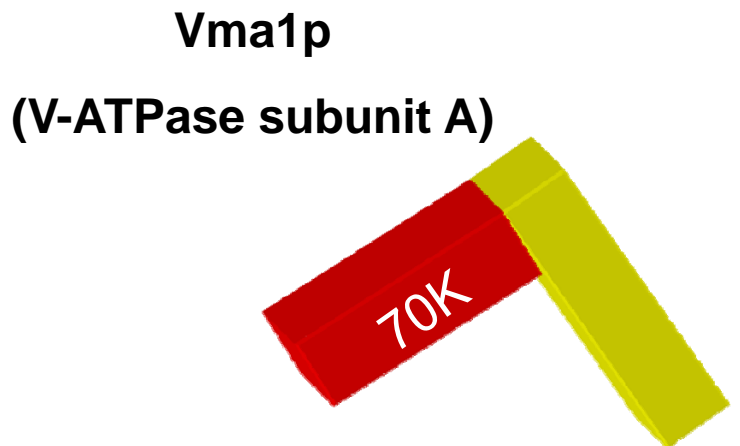
transcription

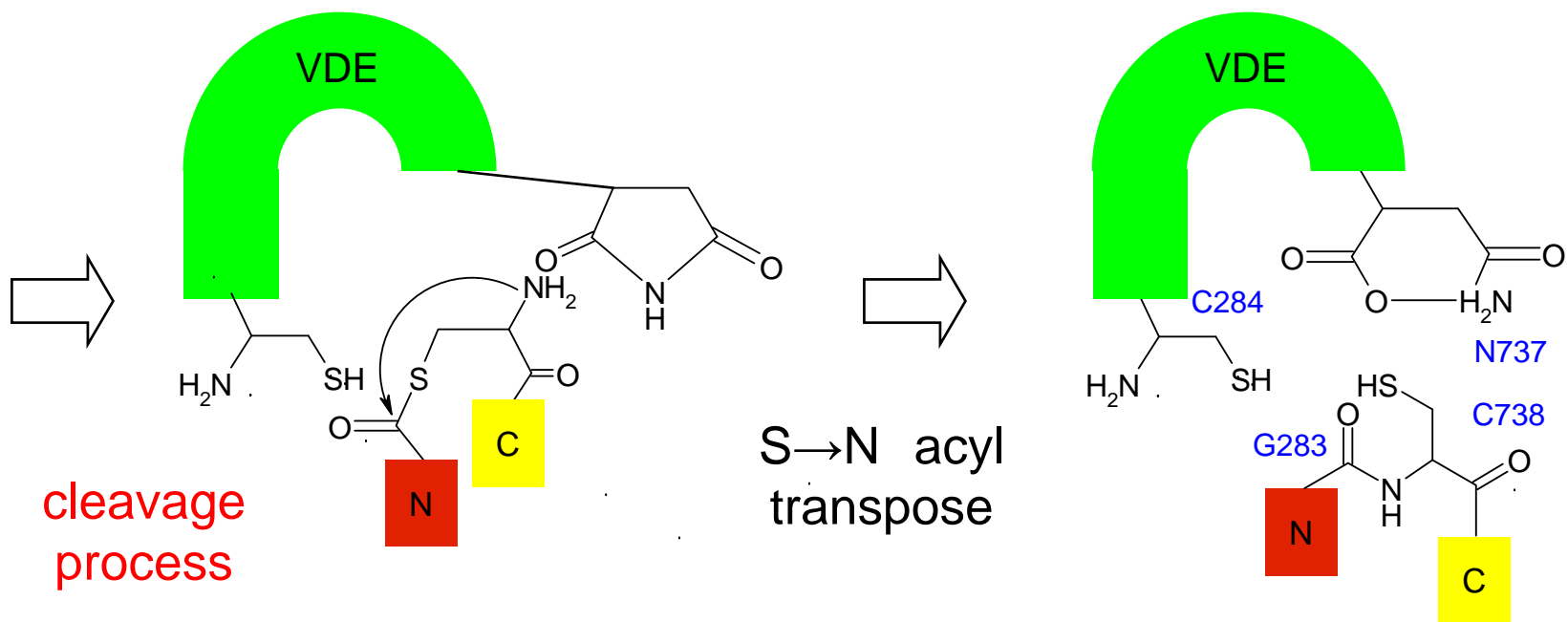
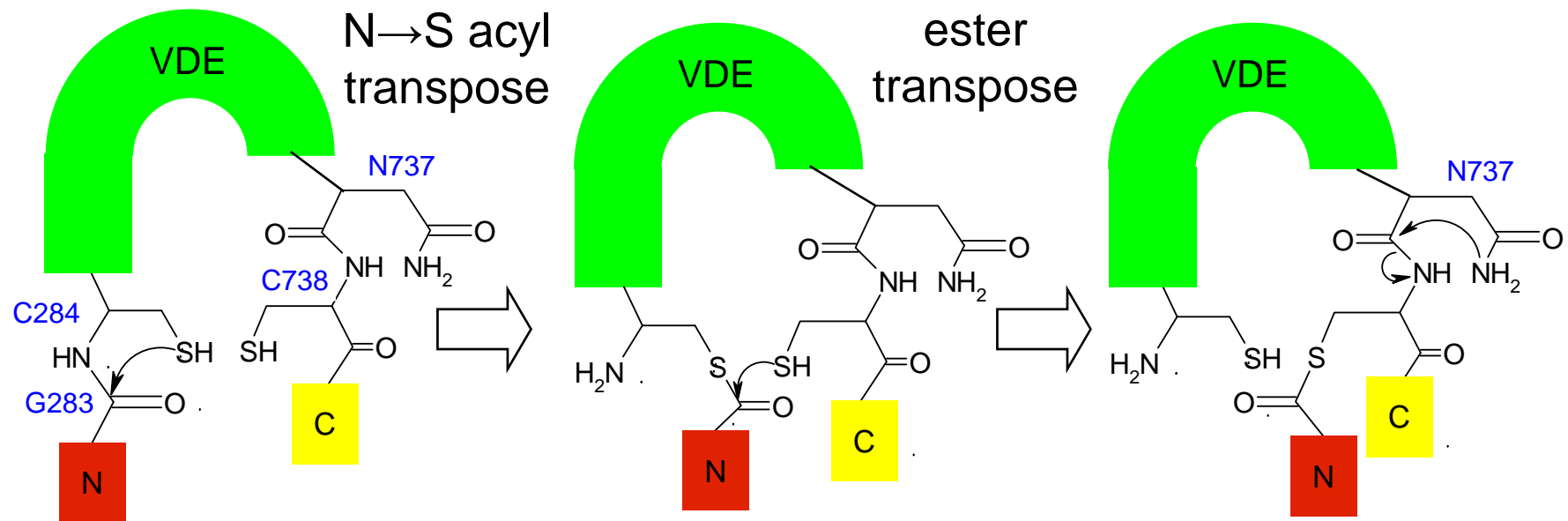


translation

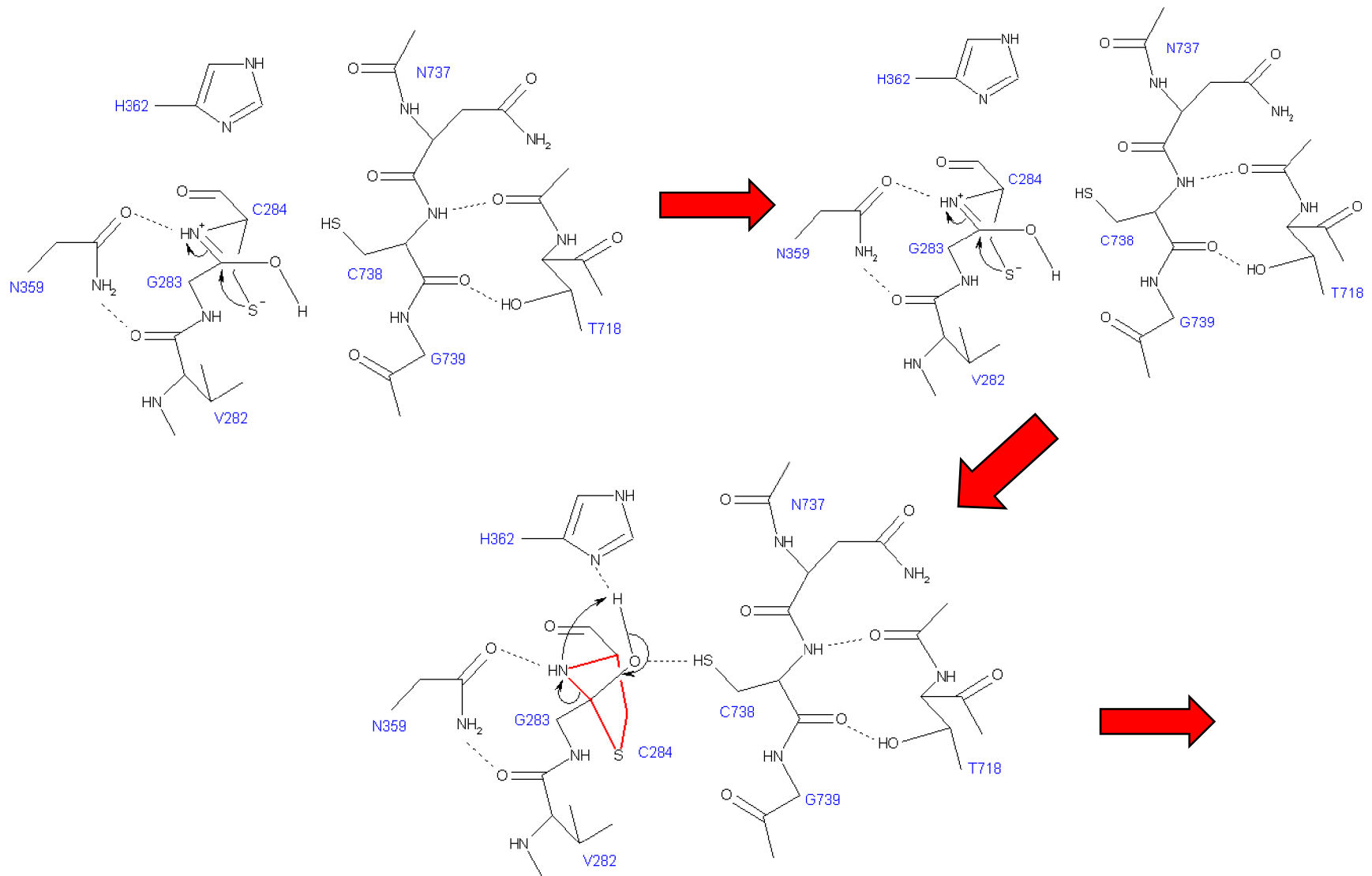


protein splicing

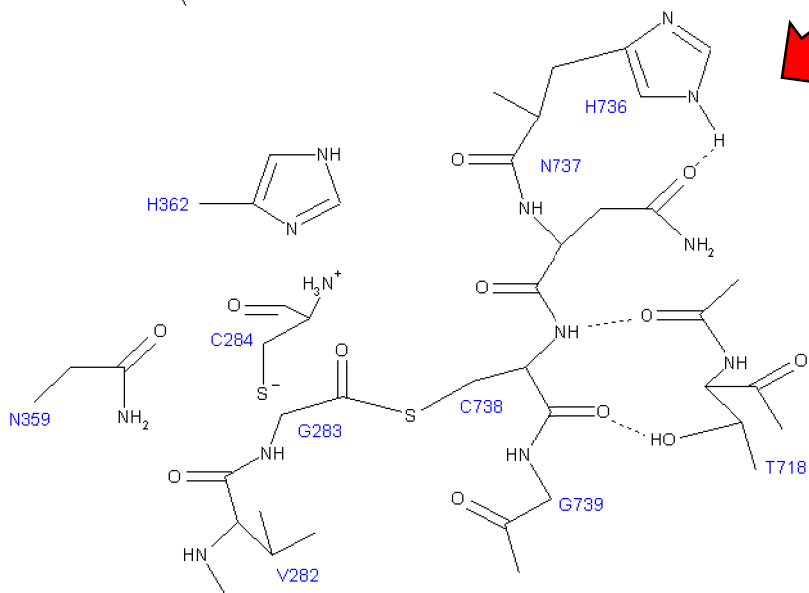
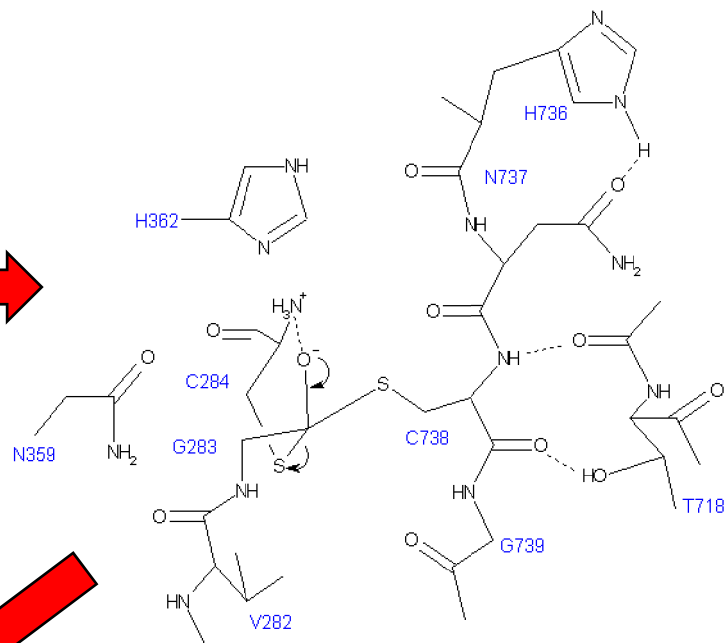
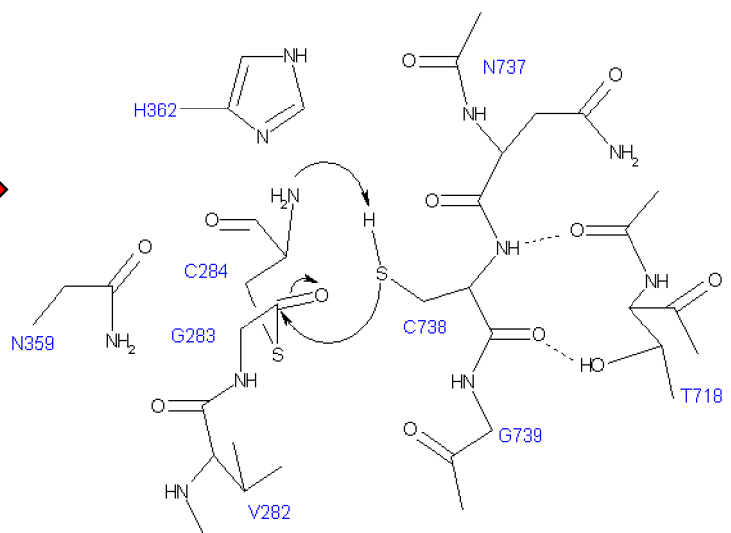
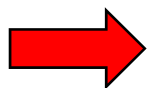




# N→S acyl transpose...



# ...ester transpose



final imid-acid  
formation

# Size Problem: hybrid QM/MM approach

$$H^{tot} = H^{CP/DFT} + E^{int}[\rho, \{\mathbf{r}_i\}] + H^{MM}$$

Pure QM interaction

$$N_{el} \times N_G \times N_G$$

with

$$\psi_j(\mathbf{x}) = \sum_{\mathbf{G}} c_j(\mathbf{G}) e^{i\mathbf{G}\mathbf{x}}$$

QM/MM interface

$$NN \times N_G$$

AMBER

# Size Problem: electrostatic interaction

**Functional form** ( $N_{cl}$  = number of **classical** atoms):

$$E^{\text{int}}[\rho(\mathbf{r}), \{q_I\}] = \sum_{I=1}^{N_{cl}} q_I \int d^3r \frac{\rho(\mathbf{r})}{|\mathbf{r} - \mathbf{r}_I|}$$

**Potential** acting on the **QM** wave functions  $\psi_i(\mathbf{x})$ :

$$\frac{\delta E^{\text{int}}}{\delta \rho} = \sum_{I=1}^{N_{cl}} \frac{q_I}{|\mathbf{r} - \mathbf{r}_I|} = V^{\text{int}}(\mathbf{r})$$

Expensive if  
 $N_{cl}$  is large !

**Forces** acting on the **MM** charged atoms:

$$\frac{\partial E^{\text{int}}}{\partial \mathbf{r}_I} = -q_I \int d^3r \frac{\rho(\mathbf{r})}{|\mathbf{r} - \mathbf{r}_I|^3} (\mathbf{r} - \mathbf{r}_I) = \mathbf{F}_I^{\text{int}}$$



# Size Problem: reduce the computational cost

Divide the world in 3 domains

- 1) Close to the **QM** region ( $\mathbf{r} < \mathbf{r}_1$ )
- 2) Not too far, i.e. **ESP** region  
( $\mathbf{r}_1 < \mathbf{r} < \mathbf{r}_2$ )
- 3) Far **MM** world ( $\mathbf{r} > \mathbf{r}_2$ )

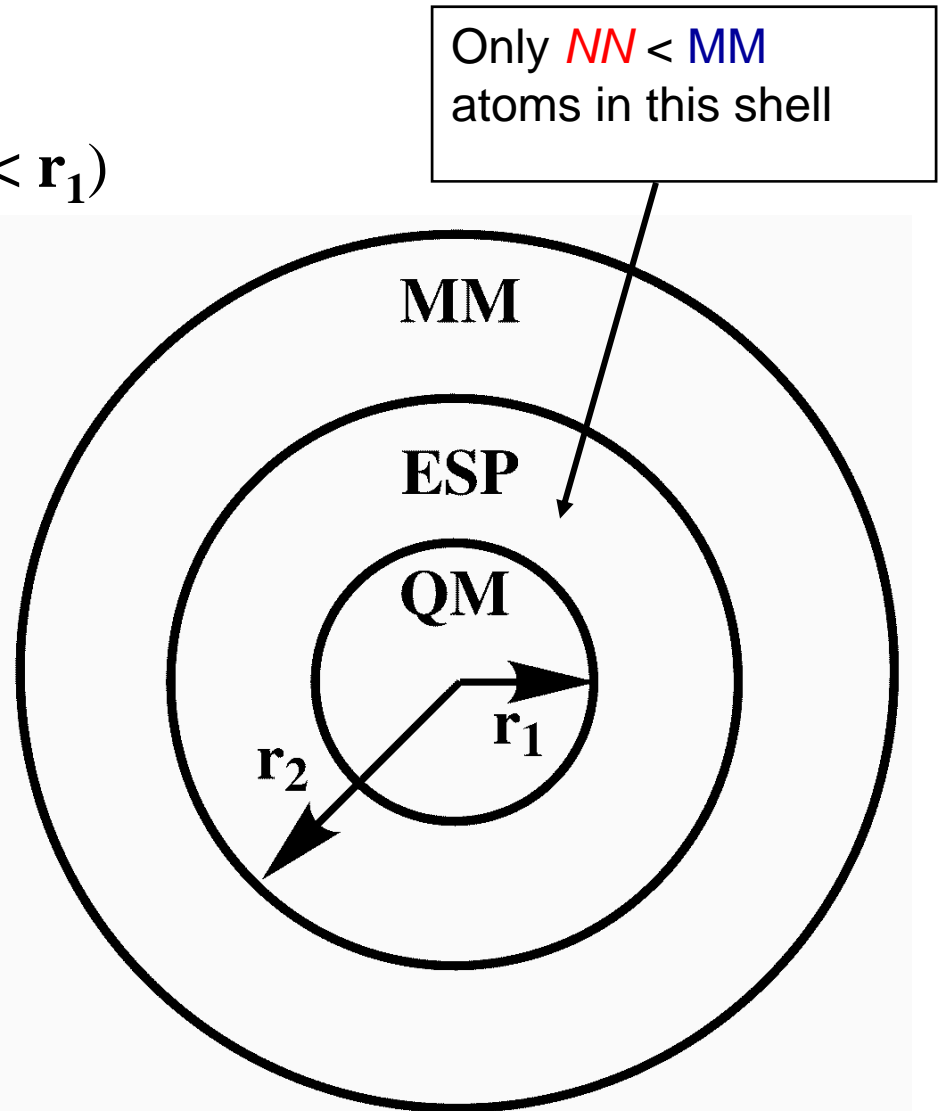
Test with  $r_1 = r_2 = \infty$



In all known cases (so far)

$\mathbf{r}_1 \sim 10\text{-}12$  a.u.

$\mathbf{r}_2 \sim 20\text{-}25$  a.u.



# Size Problem: 3-regions scheme

Region 1:  $NN \ll Ncl$



only a **subset** of  $Ncl$

$$\sum_{I=1}^{NN} q_I \int d^3r \frac{\rho(\mathbf{r})}{|\mathbf{r} - \mathbf{r}_I|} \quad r < r_1$$

Region 2: Classical-**RESP** charges interaction:

$$\sum_{I \in NN} q_I \sum_{J \in QM} \frac{q_J^{RESP}(\rho, \mathbf{r}_I)}{|\mathbf{r}_I - \mathbf{r}_J|} \quad r_1 < r < r_2$$

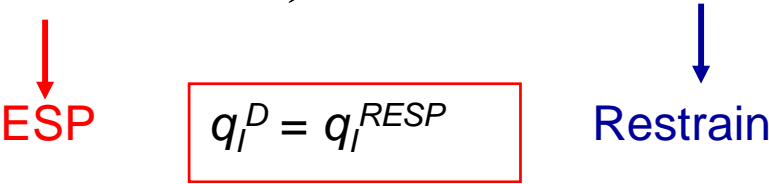
Region 3: Multipolar expansion on **MM** charges:

$$\sum_{I \in NN} q_I \sum_{\alpha} \frac{\wp^{\alpha}(\rho)(\mathbf{r} - \mathbf{r}_I)^{\alpha}}{|\mathbf{r} - \mathbf{r}_I|^3} + \text{quadrupole} \quad r > r_2$$

# Size Problem: Dynamical – Restrained Electrostatic Potential (D-RESP)

- Ask the D-RESP potential to be as close as possible to the true **e**lectro**s**tatic **p**otential (**ESP**)  $V_J$
- **R**estrain the charge (**R-ESP**) to avoid unphysical dynamical fluctuations

$$\chi = \sum_{J \in NN} \left( \sum_{I \in QM} \frac{q_I^D}{|\mathbf{r}_I - \mathbf{r}_J|} - V_J \right)^2 + w_q \sum_{I \in QM} (q_I^D - q_I^H)^2$$



ESP  $q_I^D = q_I^{RESP}$  Restrain

## Size Problem: dynamic RESP charges ( $q_I^D$ )

$$\chi = \sum_{J \in NN} \left( \sum_{I \in QM} \frac{q_I^D}{|\mathbf{r}_I - \mathbf{r}_J|} - V_J \right)^2 + w_q \sum_{I \in QM} (q_I^D - q_I^H)^2$$

is minimized *on the fly* during the dynamics.

$w_q$  = weight parameter to reduce charge fluctuations

$$w_q \approx 0.10 - 0.25$$

$$V_J = \int d^3r \rho(\mathbf{r}) u(|\mathbf{r} - \mathbf{r}_J|)$$

$u(|\mathbf{r} - \mathbf{r}_J|)$  = Coulomb potential modified at short range to avoid spurious over-polarization effects

A. Laio et al. *J. Phys. Chem. B* **106**, 7300 (2002)

# Size Problem: the charge restraint

$$w_q \sum_{I \in QM} (q_I^D - q_I^H)$$

$q_I^H$  are the **Hirshfeld charges**\* (F. L. Hirshfeld, *Theo. Chim. Acta* **44**, 129 (1977))

$$q_I^H = \int d^3r \rho(\mathbf{r}) \frac{\rho^{at}(|\mathbf{r} - \mathbf{r}_I|)}{\sum_K \rho^{at}(|\mathbf{r} - \mathbf{r}_K|)} - Z_I$$

$\rho^{at}$  is the **atomic** (pseudo) **valence charge density** and

$$Z_I = \int d^3r \rho^{at}(\mathbf{r} - \mathbf{r}_I) \quad \Rightarrow \quad \boxed{\text{valence of the } I\text{-th atom}}$$

# Size Problem: RESP coupling potential

$$V^{RESP}(\rho, \{q_J\}) = \sum_{J \in NN} \sum_{I \in QM} \frac{q_J q_I^D}{|\mathbf{r}_I - \mathbf{r}_J|}$$

replaces the **more expensive**  $\sum_J q_J \int d^3 r \rho(\mathbf{r}) u(|\mathbf{r} - \mathbf{r}_J|)$

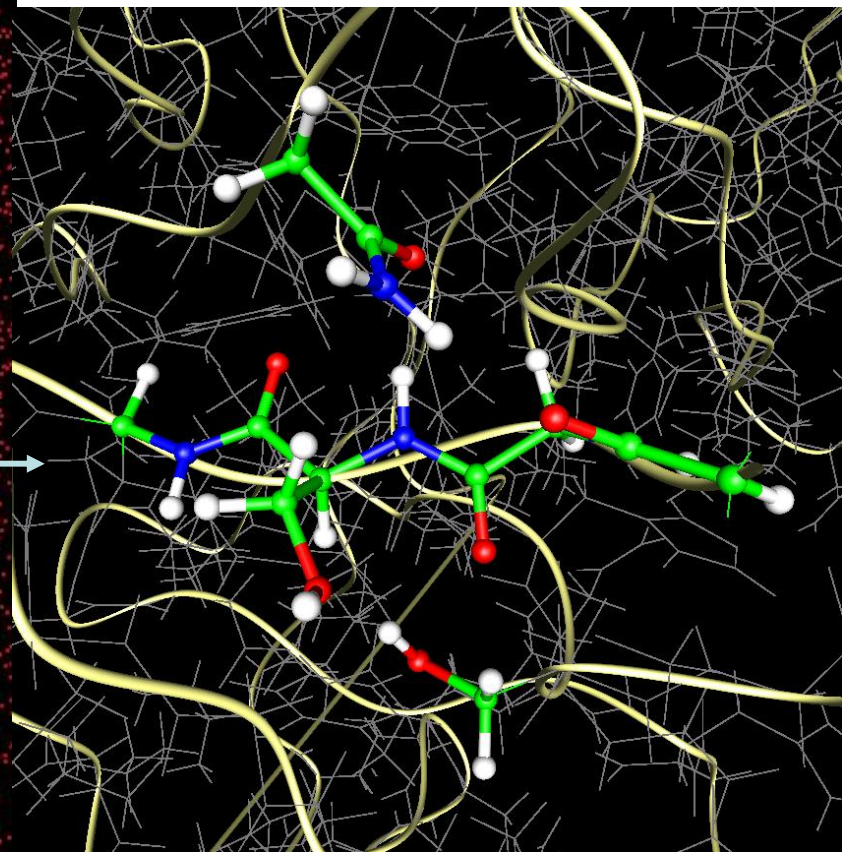
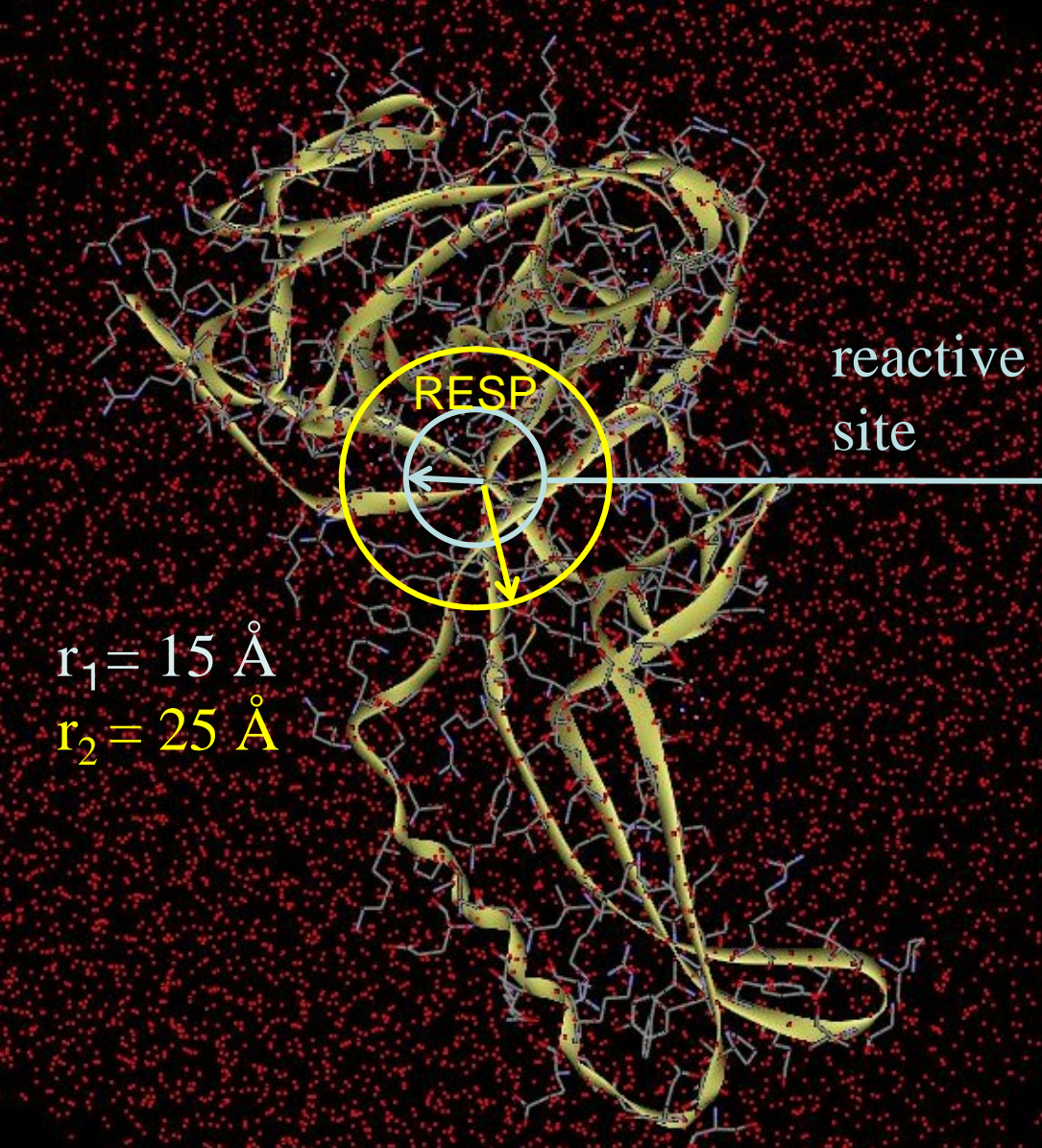
Coupling potential on electrons:

$$v(\mathbf{r}) = \frac{\delta V^{RESP}}{\delta \rho(\mathbf{r})} = \sum_{I \in QM} \frac{\partial V^{RESP}}{\partial q_I^D} \frac{\delta q_I^D}{\delta \rho(\mathbf{r})}$$

Forces components on atoms:

$$\mathbf{F}_J = -\nabla_{\mathbf{r}_J} V^{RESP} = -\frac{\partial V^{RESP}}{\partial \mathbf{r}_J} - \sum_{I \in QM} \frac{\partial V^{RESP}}{\partial q_I^D} \frac{\partial q_I^D}{\partial \mathbf{r}_J}$$

Details in M.B. and M. Tateno, in *Modelling Structure and Reactivity in Biological Systems* ed. by J. J. Naidoo, J. Brady, M. Field, J. Gao and M. Hann, RSC Publishing, Cape Town, July 2006.



## Protein in solution

MM: 46331 atoms

QM: 45 atoms

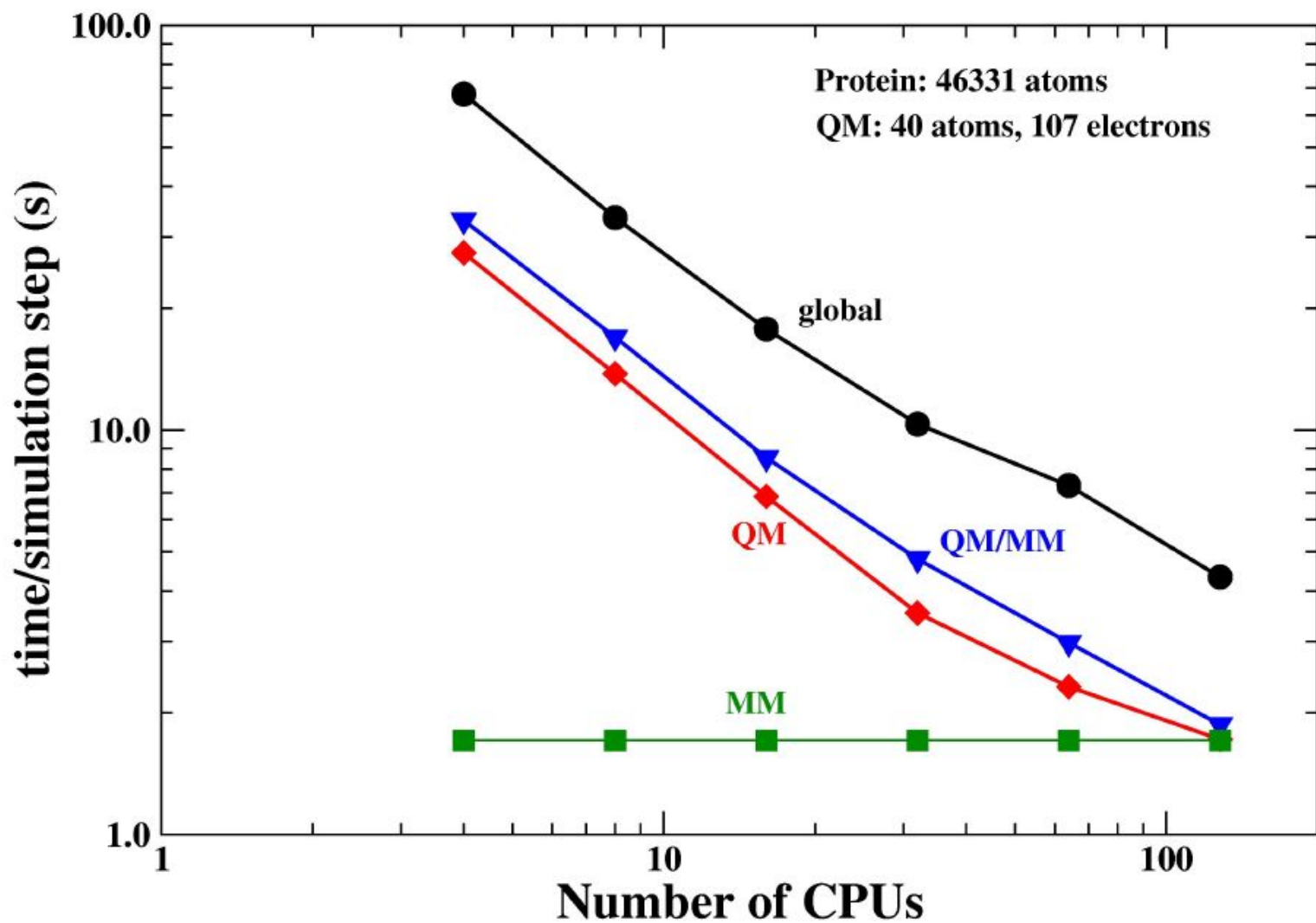
LSD-HCTH

$E^{\text{cut}}=80 \text{ Ry}$  124  $e^-$

447866 PWs

Cell=22.3 x 22.3 x 22.3  $\text{\AA}^3$

# QM/MM test on PACS-CS: 1 simulation step vs. N. of CPUs





## Performance on PACS-CS:

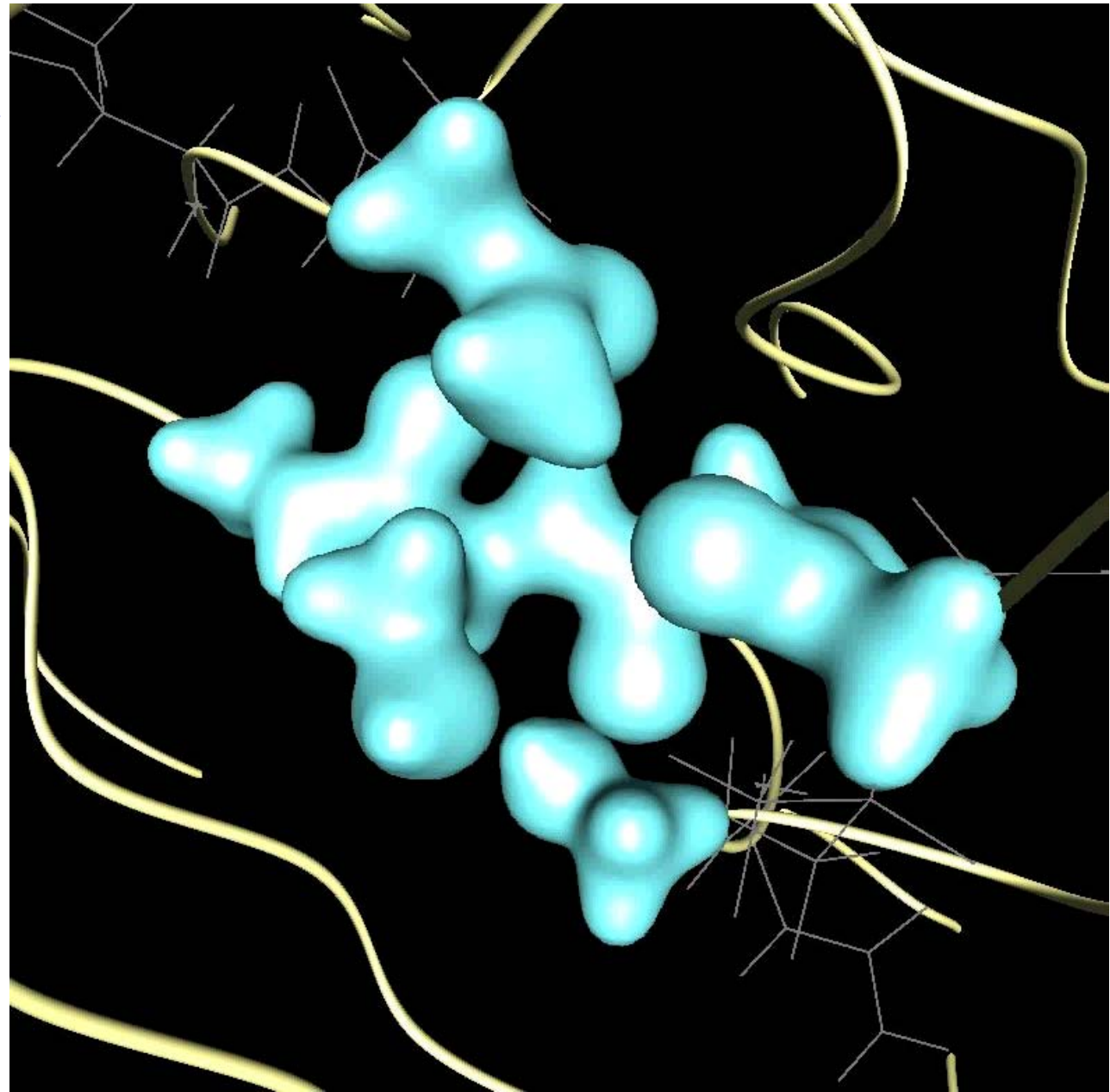
COMMUNICATION TASK	MESSAGE LENGTH	NUMBER OF CALLS
SEND/RECEIVE	17590 BYTES	253215
BROADCAST	155331 BYTES	75686
GLOBAL SUMMATION	42865 BYTES	108057
ALL TO ALL COMM	227932 BYTES	306103

	PERFORMANCE	TOTAL TIME
SEND/RECEIVE	62.873 MB/S	70.844 s
BROADCAST	63.205 MB/S	186.003 s
GLOBAL SUMMATION	53.317 MB/S	694.990 s
ALL TO ALL COMM	23.947 MB/S	2913.515 s
SYNCHRONISATION		22.136 s

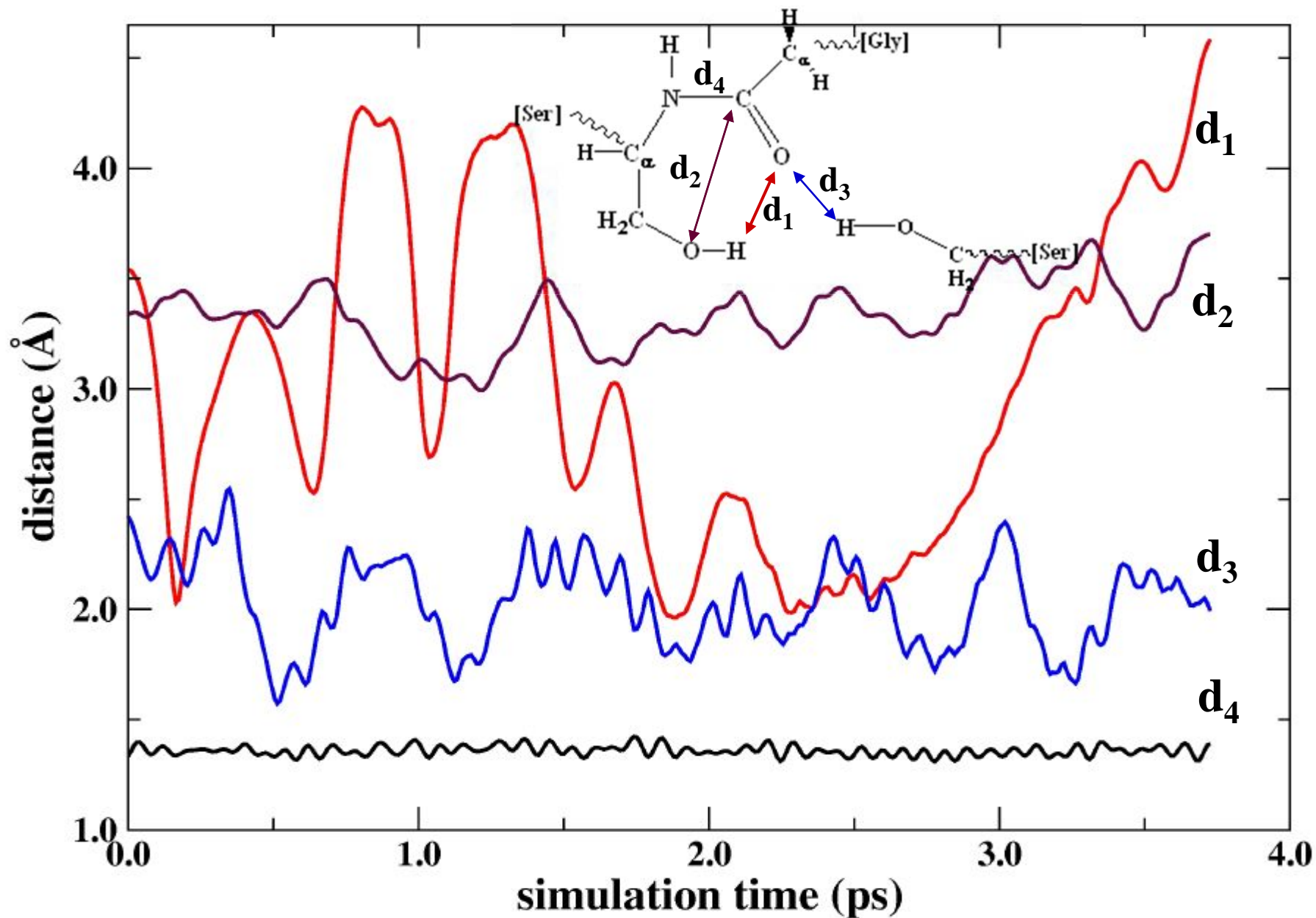
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PEAK MEMORY 25221396 = 201.8 MBytes

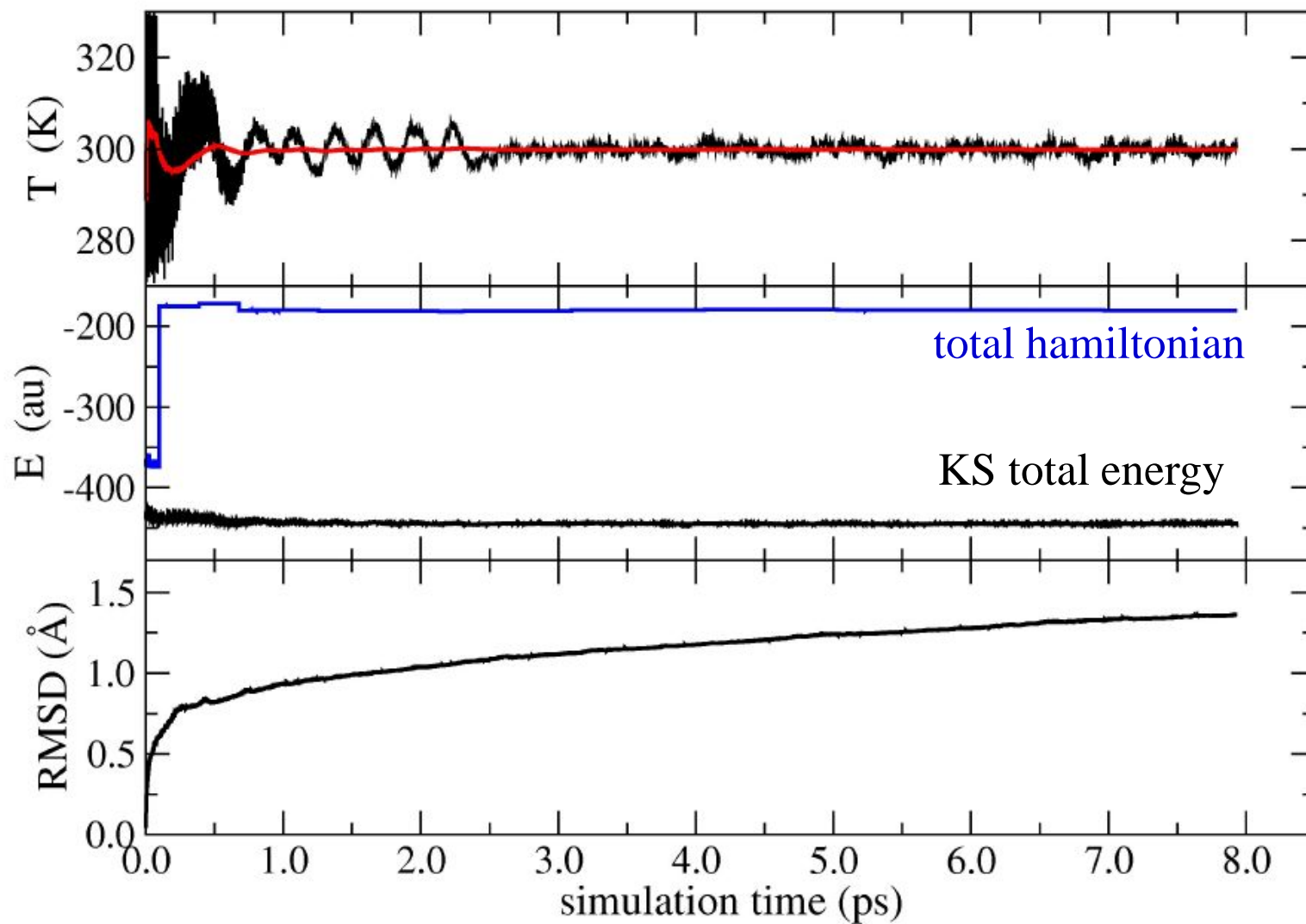
CPMD equilibration  
(after 40 ps of classical  
AMBER-MD)



# CPMD equilibration (after 40 ps of classical AMBER-MD)



# CPMD equilibration (after 40 ps of classical AMBER-MD)



# Metadynamics: collective variables and related simulation parameters

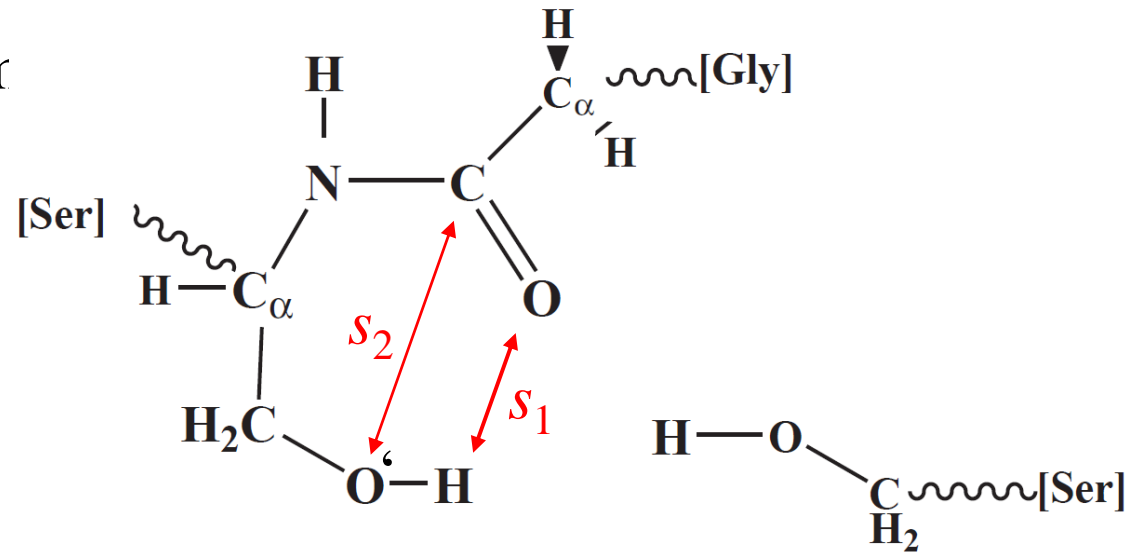
Simulation 1:  $s_1 = |\text{O} - \text{H}|$  &  $s_2 = |\text{O}' - \text{C}|$  (forming two new bonds)

$$M_\alpha = 20.0 \text{ a.u.}$$

$$k_\alpha = 0.24 \text{ a.u.}$$

$$\max\{W_i\} = 0.25 \text{ kcal/r}$$

$$\Delta s^\perp = 0.12$$



# Metadynamics: collective variables and related simulation parameters

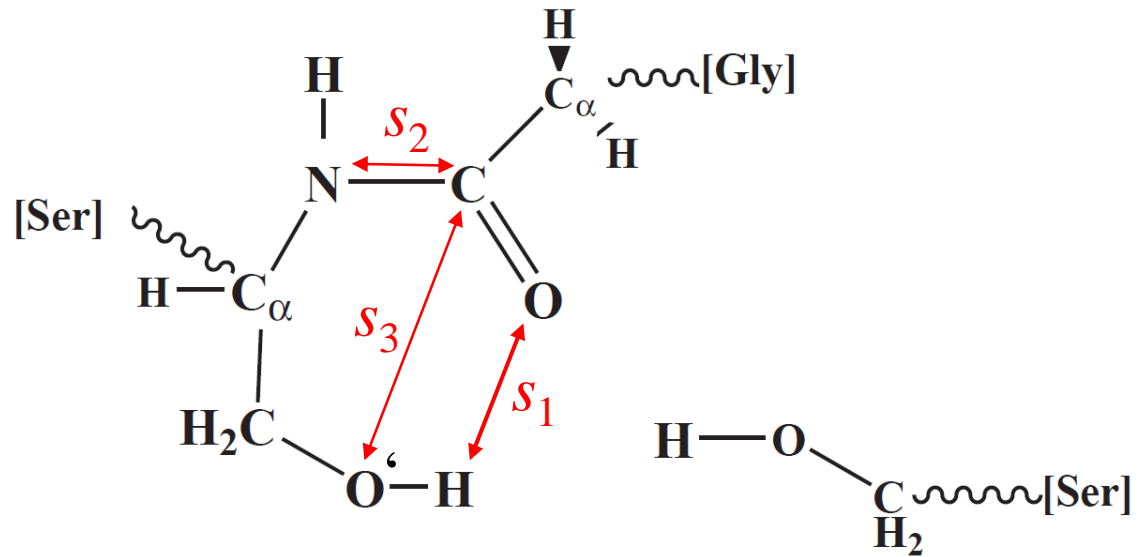
Simulation 2:  $s_1 = |\text{O}-\text{H}|$ ,  $s_2 = |\text{N}-\text{C}|$  &  $s_3 = |\text{O}'-\text{C}|$   
(breaking of the **N-C** bond included)

$$M_\alpha = 20.0 \text{ a.u.}$$

$$k_\alpha = 0.24 \text{ a.u.}$$

$$\max\{W_i\} = 0.25 \text{ kcal/mol}$$

$$\Delta s^\perp = 0.12$$





## Conclusions (so far):

- OH groups of the catalytic site can break and reform H-bonds easily
- Other moieties are more rigid and do not show significant conformational changes on ns (MM) and ps (QM/MM) time scales
- Reactive complex obtained in the equilibration stage
- Accurate analysis of the electronic structure of the protein splicing site with explicit solvent

## Related recent publications:

M. Boero, T. Ikeda, E. Ito and K. Terakura, *J. Am. Chem. Soc.* **128**, 16798 (2006)

T. Ikeda, M. Boero and K. Terakura, *J. Chem. Phys.* **127**, 074503 (2007)

K. Kamiya, M. Boero, M. Tateno, K. Shiraishi and A. Oshiyama, *J. Am. Chem. Soc.* **129**, 9663 (2007)

M. Boero, *J. Phys. Chem. A* **111**, 12248 (2007)

Y. Komeiji, T. Ishida, D.G. Fedorov, and K. Kitaura, *J. Comput. Chem.* **28**, 1750 (2007)