



Liverpool Lattice Group:
Flavour singlet spectrum

Alan Irving

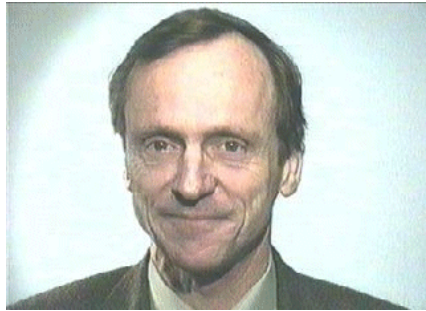
University of Liverpool



1. **Who's who in the Liverpool lattice group**
2. **Flavour singlet physics with Wilson quarks**
3. **Singlet physics with Improved Staggered quarks**
4. **Conclusions and outlook**

Who's who

Liverpool



Chris Michael

Light hadrons
Singlets (wilson)
Heavy quarks



Alan Irving

Light hadrons
Singlets (stagg)
Grid



Paul Rakow

Structure fns
Overlap



Craig McNeile

Light/Heavy quarks
Singlets, Grid,
Software...



Zbyszek Srockzinski

Phys/programmer



Stewart Wright (← *Eric Gregory*)

Chiral extrapol methods



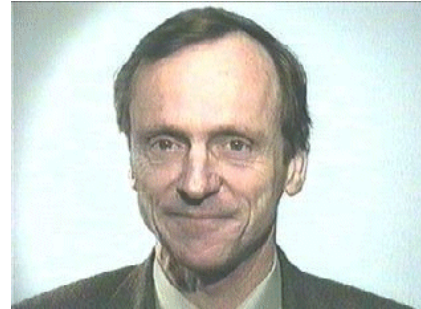
Steve Miller

Gballs, scalars

Singlet physics with Wilson quarks

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Chris Michael, Craig McNeile, ...



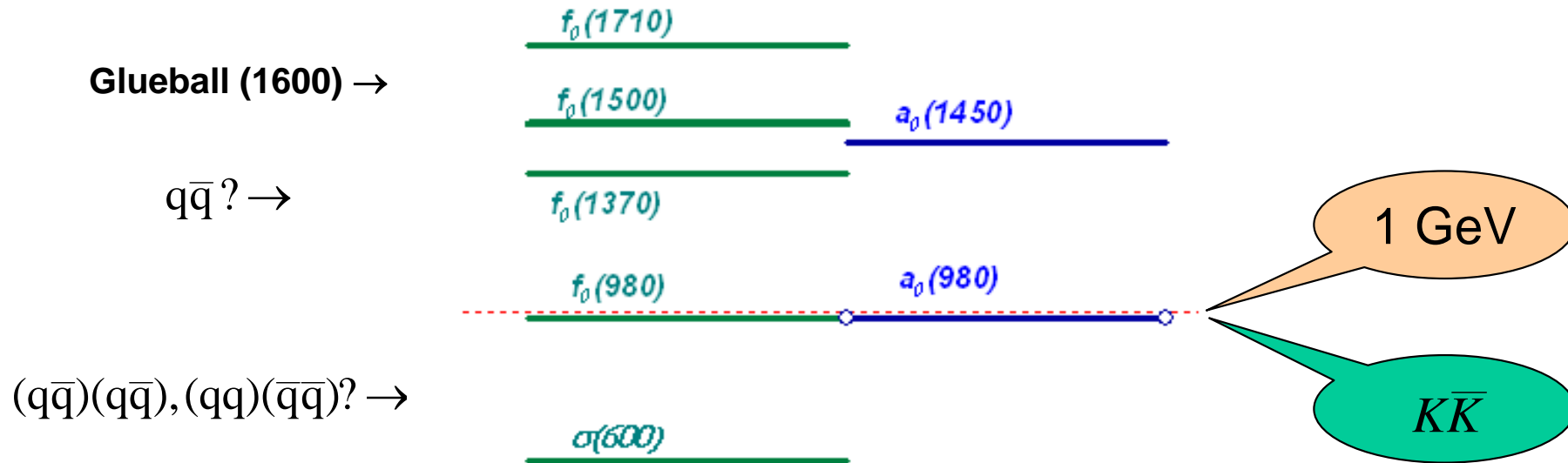
Some history:

- Phys.Rev.D63:114503,2001, **Glueball-scalar mixing**
- Phys.Lett.B491:123-129,2000, Err.B551:391,2003, **$\eta - \eta'$ mixing**
- Phys.Rev.D65:014508,2002 (+ K Sharkey), **Scalar mesons**
- Nucl.Phys.Proc.Suppl.119:266-268,2003 (+ A Hart), **Scalar particles**

- Concentrate on 0^{++} states
- Pure glue requires order 10^4 configs $\rightarrow m(0^{++}) \sim 1600$ MeV
- Benefits from asymmetric actions (Morningstar and Peardon)
- Interest is in the effects of **light quark** effects (meson – glueball mixing)
- Dynamical light quarks
- Simulation limitations

Experimental light scalar spectrum

- Scalars separate into 2 groups above/below 1 Gev (e.g. Close, Tornquist hep-ph/0204205, JPhysG 28 (2002) R249)



- Conventional $^3P_0 q\bar{q}$ at around 1.5 GeV?
- Unconventional $(qq)^3(\bar{q}\bar{q})^3$ nonet below 1 GeV
- ... with meson-meson component $(q\bar{q})^1(\bar{q}q)^1$?

Operators

G (glueball, gluon loop)

L (quark loop)

M (meson/connected)

Full theory

$$\langle G(0)G(t) \rangle$$

$$\langle G(0)L(t) \rangle$$

$$\langle L(0)G(t) \rangle$$

$$\langle L(0)L(t) \rangle$$

$$\langle M(0)M(t) \rangle$$

D(t)

C(t)

Quenched

- no sea quark loops L
- M and G states are distinct, C(t) is same for S and NS scalars
- (valence) mixing matrix element estimate $\langle LG \rangle$ (McN & M)
- care: anomalous contributions from 0^-0^- interm. states

Glueballs (G)

- APE smearing (2 levels) + Teper blocking (3 levels) of spatial links
- Time plane sums for scalar operators for $|p|=0,1$
- Tensor operators for $|p|=0$ only

Connected mesons (M)

- Local and smeared/fuzzed operators from $q = M^{-1}S$

Disconnected (loop) contributions (L)

- $L = Tr(\Gamma M^{-1})$
- Stochastic estimators
- Volume sources, noise reduction techniques

- Variational techniques
- Factorising fits

Quenched results

- See PRD 63 (2001) 114503, (CMcN&CM) for quenched evaluation of mixing M.E. at the strange quark mass

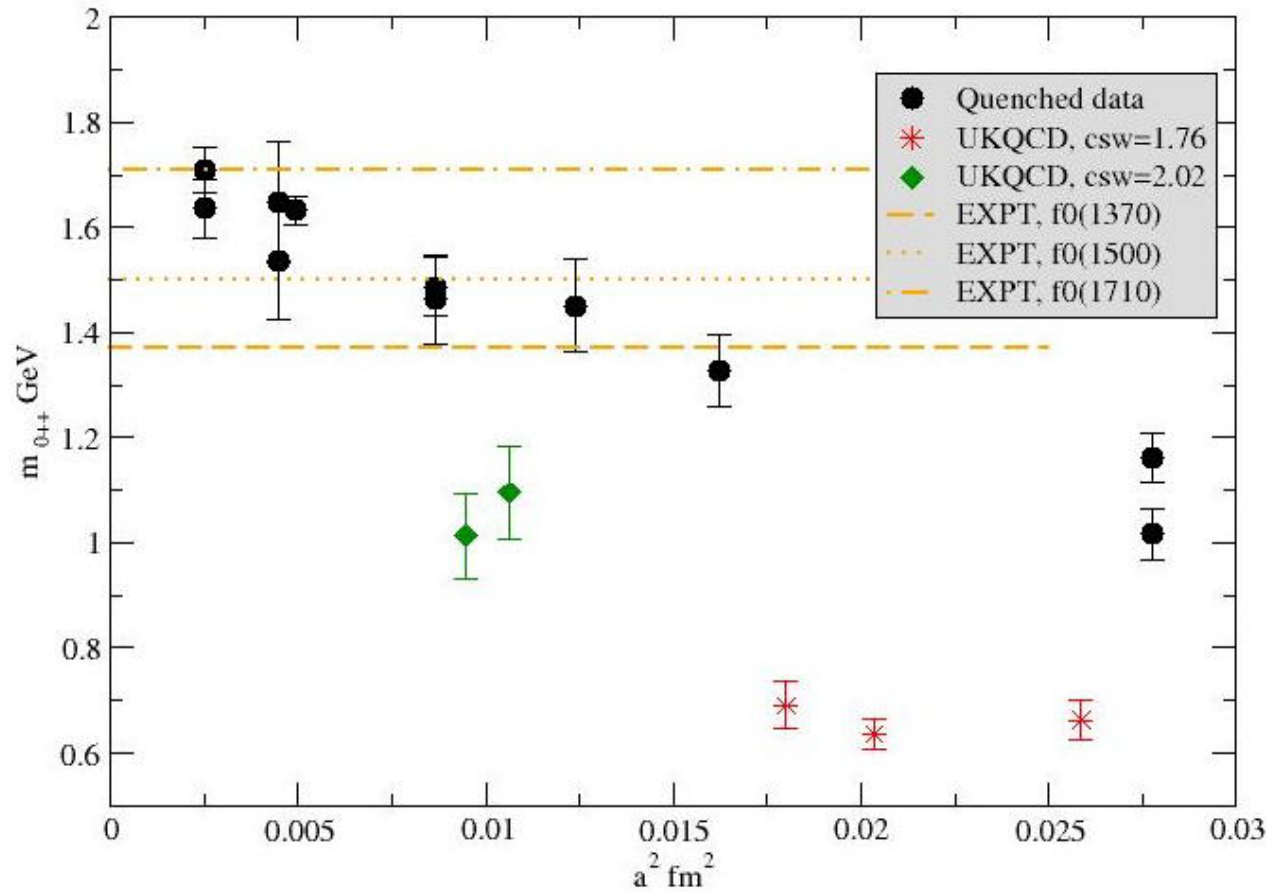
$$r_0 x_{00} \approx 0.76(12) \quad \text{for 1 flavour of strange quark}$$

Gball

$$\begin{pmatrix} am_0 & \sqrt{2}ax_{00} \\ \sqrt{2}ax_{00} & as_0 \end{pmatrix} = \begin{pmatrix} 0.95 & 0.42 \\ 0.42 & 1.39 \end{pmatrix} \rightarrow \text{eigenstates at } 0.69 \text{ and } 1.65$$

scalar meson

\Rightarrow 25% downward shift of scalar glueball in $n_f=2$ simulations?



- **Glueball: Strong a^2 dependence (Wilson gauge action)**
- **$n_f=2$ fermions ($m \sim$ strange) reduce the mass at fixed a^2 or ..**
- **.. even stronger lattice artefacts with NP- improved Wilson/clover fermions?**
- **So need:**
 - different action(s)
 - finer lattices
 - (higher statistics)

C Michael and student J Pickavance have begun an analysis of CP- PACS configs from: www.lqa.rccp.tsukuba.ac.jp

1. glueball analysis

- compare with UKQCD $n_f=2$, NP improved Wilson/clover
- is this a ‘better’ gauge action?

2. Fermion loops (+ C McNeile)

3. Mixing analysis à la McNeile & Michael

Quarks are still quite heavy ($m_\pi/m_\rho = 0.8 \rightarrow 0.6$)

Mixing ME analysis only good for heavy(ish) quarks
(on-shell transition amplitudes)

- ⇒ better to make direct measurements
- dynamical configs with lighter quarks
 - gluonic and mesonic operators



Steven Miller, ACI, CM, CMcN, ...

SM Thesis project:

- Develop singlet (glueball and meson) measurement formalism for improved staggered fermions
- Test using largest available MILC configuration ensembles.
- Measure scalars/glueballs on high statistics ensemble generated in first runs on UKQCD 'phase I' QCDOC machine.
- Use/augment SCIDAC/JLAB standard code 'Chroma' to promote future developments.

Additional applications:

- η / η'
- other processes involving disconnected contributions

Glueball measurements on MILC ensembles

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- Use MILC ensembles (at NERSC: qcd.nersc.gov) generated using the Asqtad action (Bernard et al: PR D64 (2001) 054506)

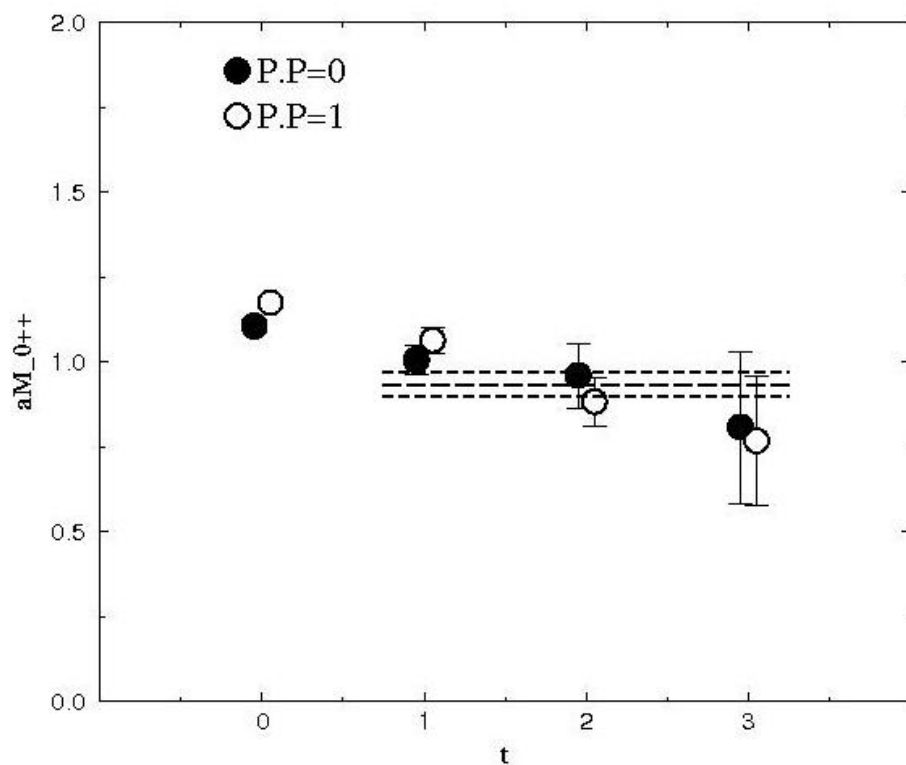
Ensemble	β	m_l/m_s	$2am_\pi$	$am_{0^{++}}$
A	6.81	.03/.05	0.755	0.934(37)(-107)
B	6.79	.02/.05	0.623	1.099(45)(-132)
C	6.76	.01/.05	0.449	0.927(41)(-120)
D	6.76	.007/.05	0.378	0.801(41)(-188)
E	7.11	.0124/.031	0.413	0.740(48)(-60)
F	7.09	.0062/.031	0.296	0.716(54)(-61)

$a \sim 0.125$ fm

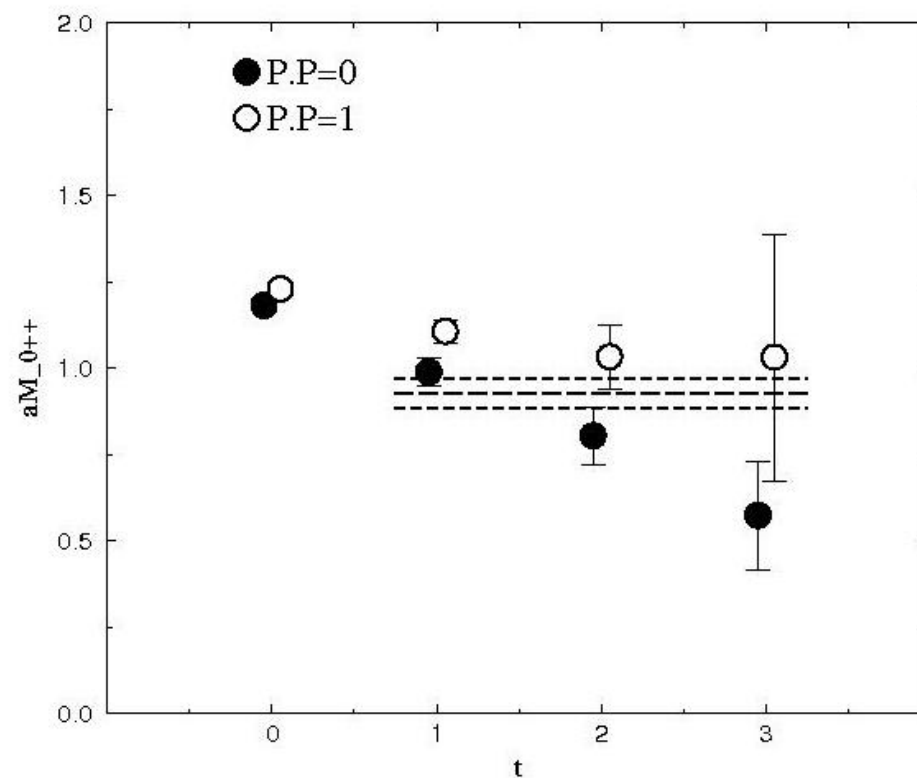
$a \sim 0.09$ fm

Effective mass plots for scalar glueball

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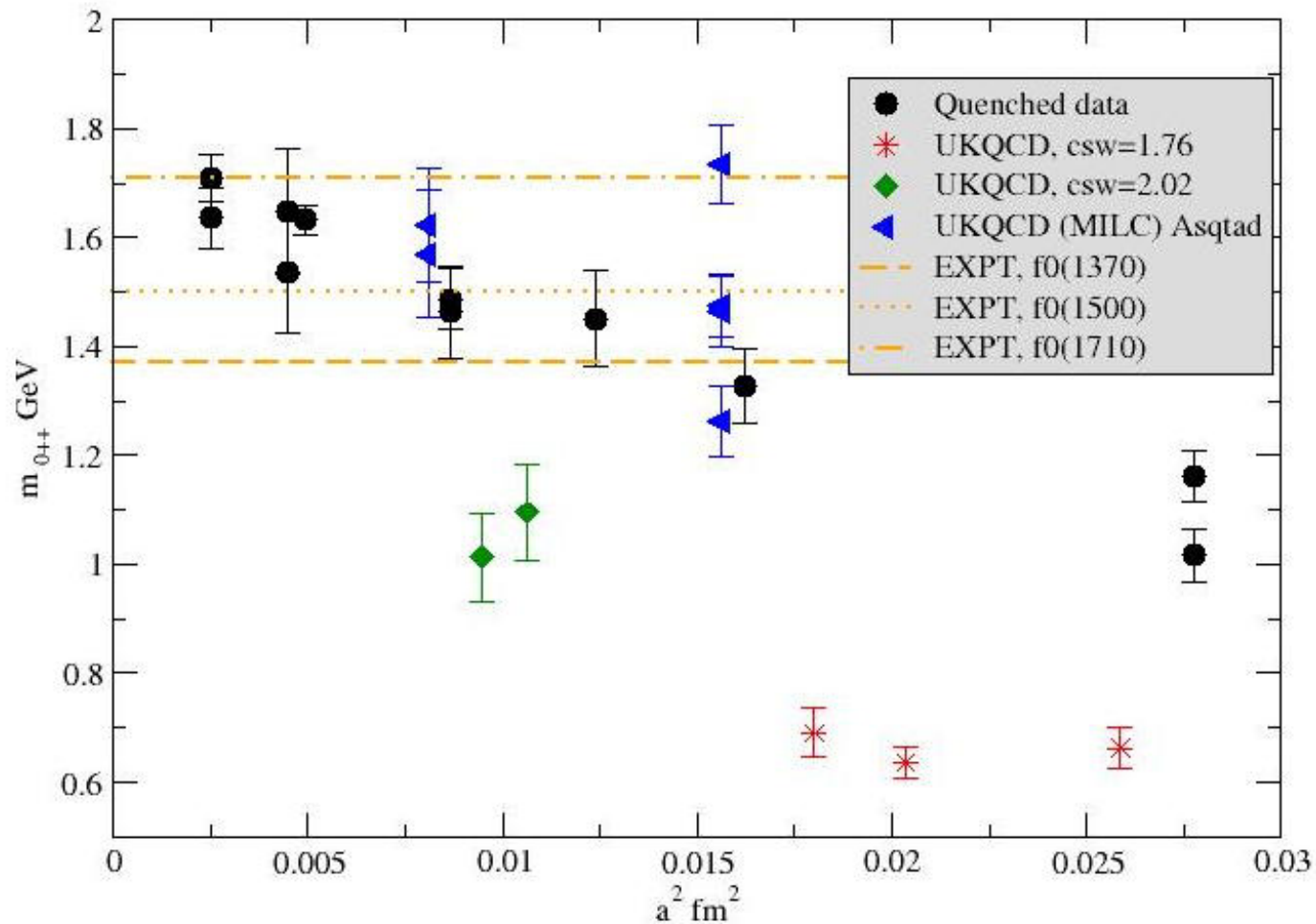
$\beta = 6.81$, $m_l/m_s = 0.03/.05$
(564 configs) $a = .12$ fm



$\beta = 6.76$, $m_l/m_s = 0.01/.05$
(658 configs) $a = .12$ fm

Staggered results for O^{++} using glueball operators only

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- Less suppression at fixed a^2 than Wilson
- Downward drift with lighter quark mass

- Unlike previous analyses, quarks are light enough for scalar glueball/meson to decay into two pions.
- Need 'proper' treatment of decays...
- .. since dynamical quarks are light enough to induce mixing.
- $O(500)$ configs is not really enough (c.f. 10,000 for pure gauge)
- Add in scalar meson operators.
- What about staggered complications?

Staggered scalar operators

- ‘Taste’ violations \rightarrow 4 x each quark flavour ($O(a^2) \rightarrow$ improvement..)
- $(\det M)^{n_f/4}$ to ‘correct’ sea quark activity in vacuum (some say ‘dodgy’?)

- Valence meson operators give 16 copies (spin \otimes taste basis):

$$O = \bar{Q}(\Gamma_s \otimes \Gamma_T)Q$$

- e.g. Goldstone pion $\gamma_5 \otimes \gamma_5$
- But $O = \bar{Q}(\gamma_4\gamma_5\Gamma_s \otimes \gamma_4\gamma_5\Gamma_T)Q$ also couples ...

... so ‘**oscillating states**’ of opposite parity in general for any given taste representation.

Parity partners

GB π

Pseudosc. rep.	J^{PC}	Parity partner	J^{PC}
$\gamma_5 \otimes \gamma_5$	0^{-+}	$\gamma_4 \otimes \gamma_4$	0^{+-}
$\gamma_4 \gamma_5 \otimes \gamma_4 \gamma_5$	0^{-+}	$1 \otimes 1$	0^{++}
$\gamma_5 \otimes \gamma_i \gamma_5$	0^{-+}	$\gamma_4 \otimes \gamma_i \gamma_4$	0^{+-}
$\gamma_4 \gamma_5 \otimes \gamma_i \gamma_4 \gamma_5$	0^{-+}	$1 \otimes \gamma_i$	0^{++}

Scalar

local

1-link

- Goldstone π has **exotic** parity partner
- Scalar has non – Goldstone π as parity partner

- Fits to $C(t)$ include (at least) scalar + oscillating pion (non-GB):

$$c(t) = A_0 e^{-m_s t} + (-1)^t A_1 e^{-m_\pi t} + \dots$$

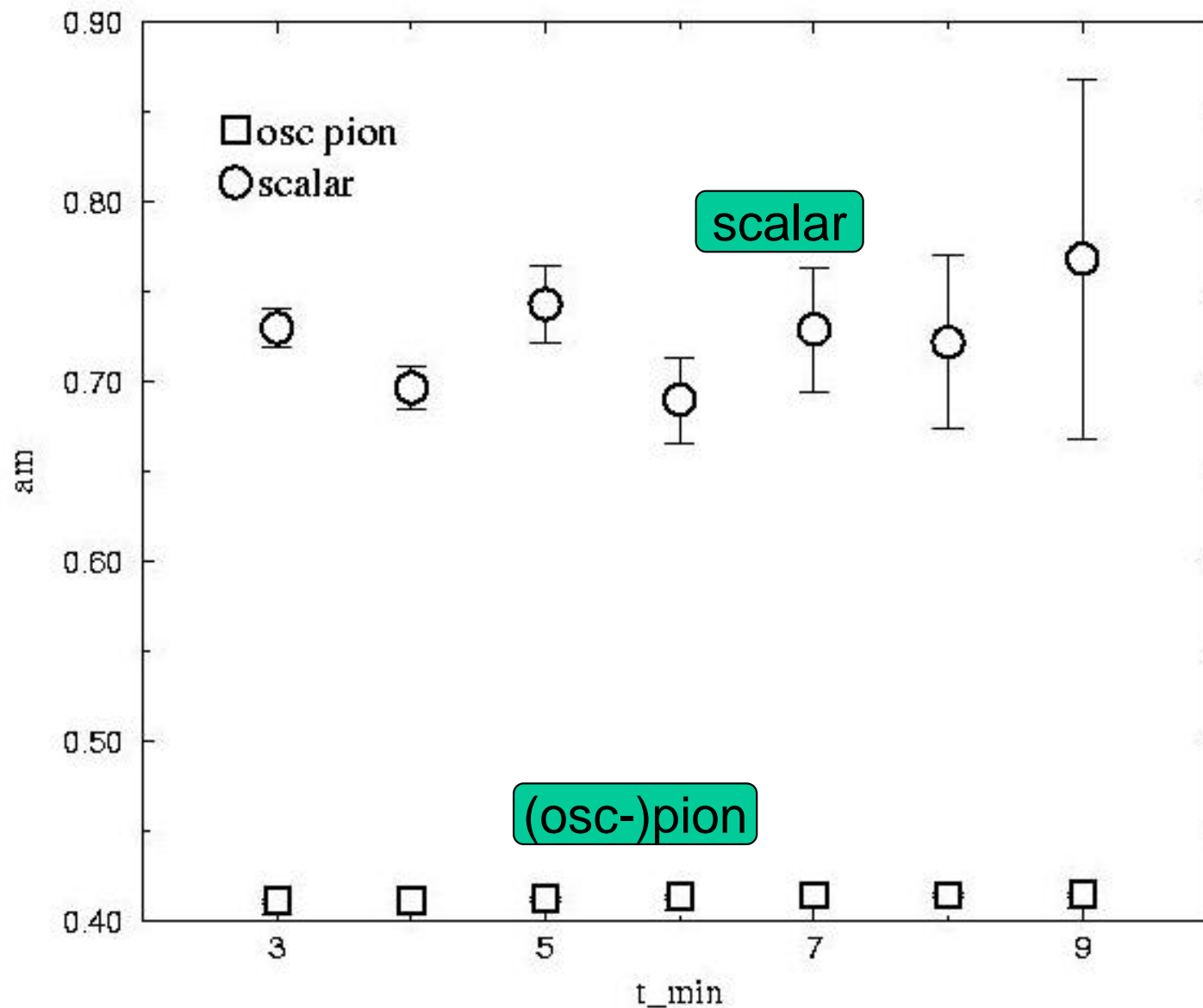
- Fuzzing used (with factorising fits) seems to help fits for the pion (and disconnected loops - see later) but NOT the scalar.
- This makes it difficult to include meaningful excited scalar and excited oscillating pion.
- Sample fits (next..)

Sample connected fits :

am_l	fit	am_π	am_{scalar}	$am_{\text{scalar (excited)}}$	χ^2/dof
.03	LL, 2 exp, t=7-20	.409(5)	.784(40)	-	1.4
	L+F factor., 3 exp, t=3-9	.399(15)	.76(15)	.96(3)	large
.01	LL, 2 exp, t=5-20	.262(31)	.549(14)	-	0.8
	L+F fact, 3 exp, t=5-14	.269(18)	.65(13)	1.03(7)	0.9

- 3 pole factorising fits not v stable (amplitude errors/correlated)
- 4 pole fit with excited (oscillating) pion even less stable.
- scalar probably needs different fuzzing (diff wave fn).

Fit range stability for local fits



Ensemble A

$am_1=0.3$

Taste violations in scalar channel

- Comparison of % taste violations with those for pion (for $m=.03$):

Operator	pion	scalar
$\gamma_5 \otimes \gamma_5$	-	-
$1 \otimes 1$	8.6(3)	-
$1 \otimes \gamma_i$	13.9(3)	6(4)
$1 \otimes \gamma_i \gamma_4 \gamma_5$	17.9(3)	9(4)
$1 \otimes \gamma_4 \gamma_5$	22.0(4)	14(5)

- $m(\text{'pi'})/m(\text{'scalar'}) \sim 1.8$
- $m(\text{rho})$ violations zero within errors

Disconnected loops $L(t)$

- Volume source with $O(50)$ (Gaussian) noise vectors
- Monitor variance w.r.t. gauge and noise

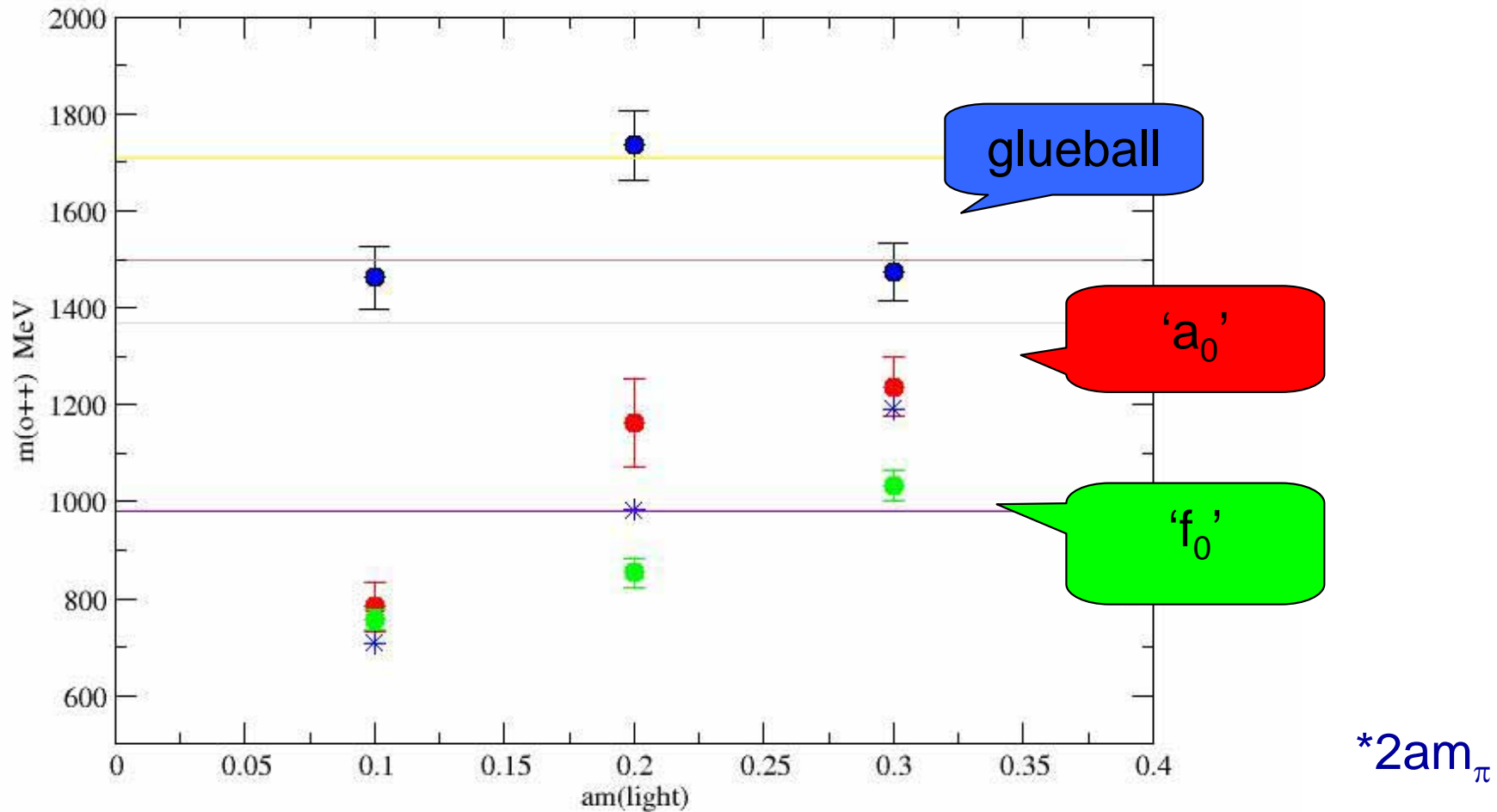
$$\text{Corr}(t) = C(t) + 2D(t), \quad D(t) = \langle L(0)L(t) \rangle$$

- The parity partner of taste singlet scalar operator is $\gamma_4\gamma_5 \otimes \gamma_4\gamma_5$
This is taste **non-singlet** so has **no** disconnected piece.
- \Rightarrow connected piece $C(t)$ has an oscillating parity partner while disconnected piece $D(t)$ does not.
- Fit strategy:
 - Fit $C(t)$ first to determine NS scalar and **0⁻** oscillating mass
 - Fit $C(t)+2D(t)$ with oscillating **0⁻** parameters fixed.
 - 2 light valence quarks only
- Fuzzing improves isolation of ground state component in $D(t)$.

Preliminary fits to MILC ensembles

Connected fit (t=3-9)			D+2C fit
am_l	m_{osc}	m_{NS}	m_{scalar}
.03	.434(12)	.784(39)	.655(20)
.02	.334(18)	.736(57)	.541(19)
.01	.241(19)	.497(32)	.479(14)

Glue and meson operator comparison (prelim)



($a \sim 0.125$ fm ensembles)

Comments on singlet meson measurements

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- For unquenched case, the complete study of the O^{++} channel should use basis consisting of various 'fuzzing' levels of:
 1. Glueball operators
 2. Connected meson contribution (ud+s)
 3. Disconnected meson contribution – loops
 4. Two pion operators
- The study reported here has so far just included **separate** fits for (1), (2) (~Non-singlet) and (2)+(3) (singlet meson) using 2 degenerate light quarks only
- Light meson operators couple to much lower mass scalar states (no real surprise there...)
- This channel is definitely **not** 'gold-plated'

Recent related work on scalars

- ‘SCALAR collaboration’ (Kunihiro et al) PRD 70 (2004) 0345
 - Coarse lattice (a ~0.2 fm, L~1.6 fm), Wilson + plaquette action
 - O(800) configs at each of 3 kappas: $m_\pi / m_\rho \approx 0.83, 0.77, 0.70$
 - Scalar singlet heavier than rho: $m_\sigma / m_\rho \approx 1.6, 1.3, 1.1$
- Prelovsek et al (hep-lat/0407037) dynamical and partially-quenched study of NS scalar using CU/BNL Domain wall dynamical configs.
 - m(a0) ~ 1.5-1.6 GeV (with large errors)
 - closer to a0(1450) than a0(980)?
 - evidence of unphysical (partial) quenching contributions

- **Choice of operators?**

$$\gamma_5 \otimes 1 \quad \text{non-local in time}$$

$$\gamma_4 \gamma_5 \otimes 1 \quad \text{3-link spatial operator}$$

- **Signal estimates for the 3-link operator**

→ 200 noise samples c.f. 50 for scalar

- Despite initial optimism, **useful** glueball measurements on dynamical configurations will probably need 10000s rather than 100s of configurations.
- One can estimate **mixing matrix elements** using quenched configurations or dynamical ones with heavy quark masses but ..
- reliable estimates of **physical** glueball/meson states require large scale dynamical simulations with realistically **light** quarks.
- Existing MILC configs using (Asqtad) improved staggered quarks may already indicate significant mixing effects and give qualitative information about the underlying singlet spectrum.
- Forthcoming higher statistics data from QCDOC should provide considerably improved insight into lattice predictions for glueball and scalar meson systems.
- First QCDOC run: $24^3 \times 64$, $a = .125\text{fm}$, $m_u/m_s = 0.01/0.039$, 20K+ trajs.