

Light Hadron Spectrum and Quark Masses in $N_f=3$ QCD

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CP-PACS/JLQCD Collabs.

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CP-PACS Collab. @CCS, Tsukuba



CP-PACS
0.6TFlops



SR8000/G1
0.2TFlops



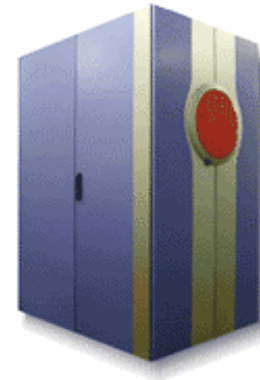
VPP5000
0.8Tflops

@ACCC

JLQCD Collab. @KEK



SR8000/F1
1.2TFlops



3% of ES

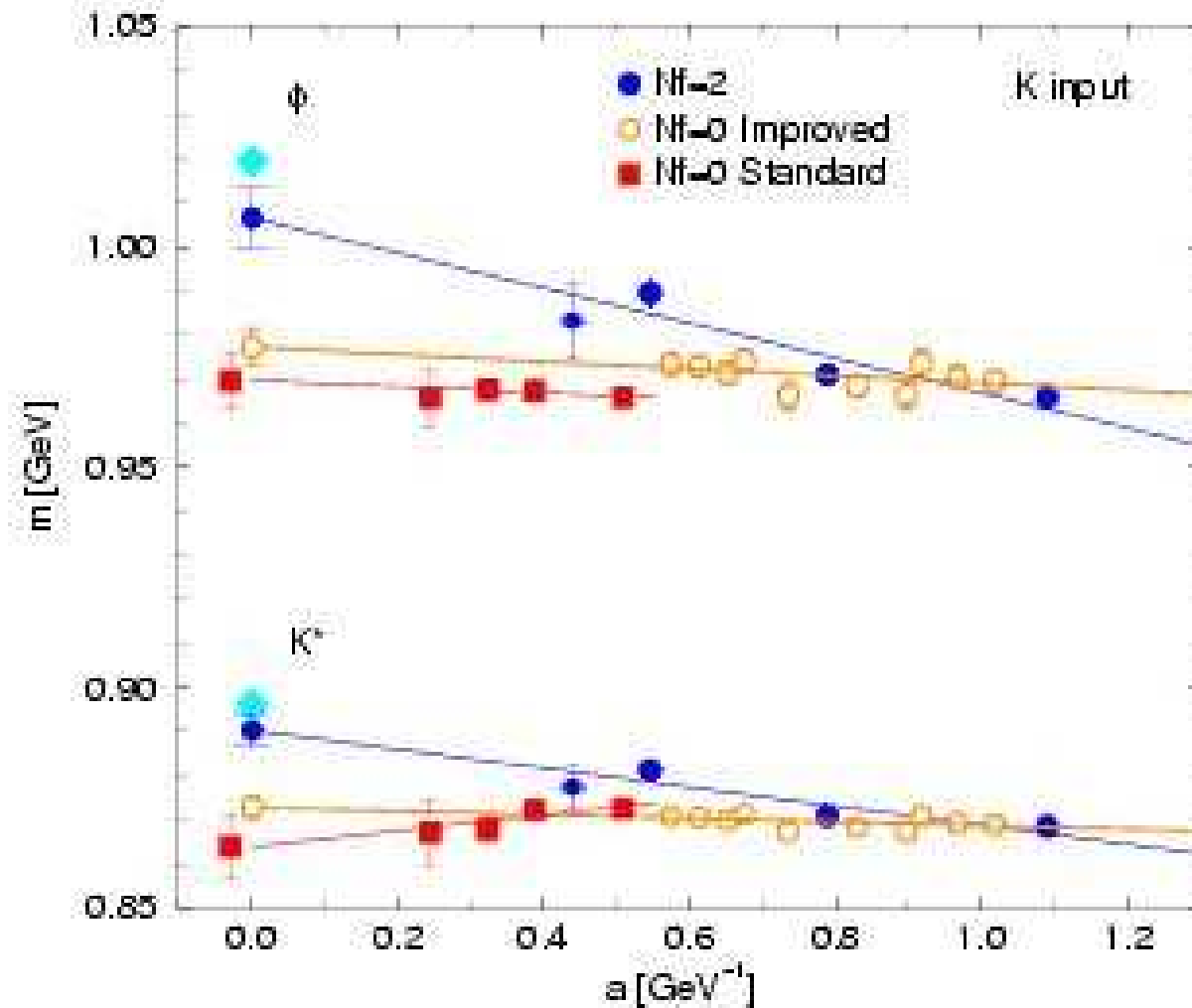
Earth Simulator
(JAMSTEC)
40TFlops

~1.5 Tflop*Year (sustained speed) in 2 years
(20-46% efficiency depending on size and machine)

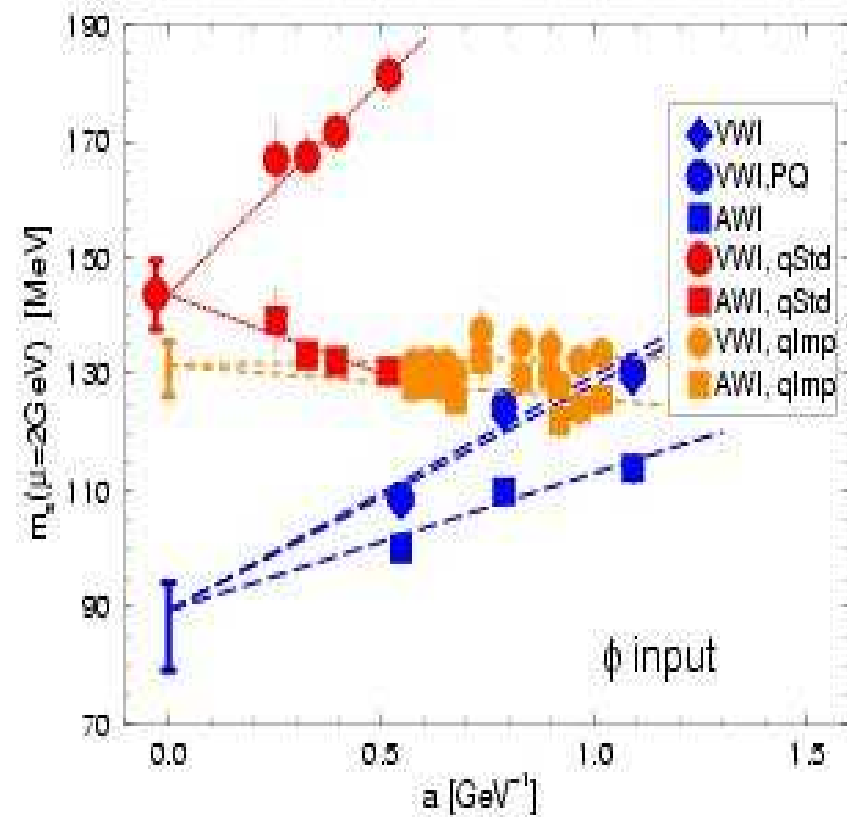
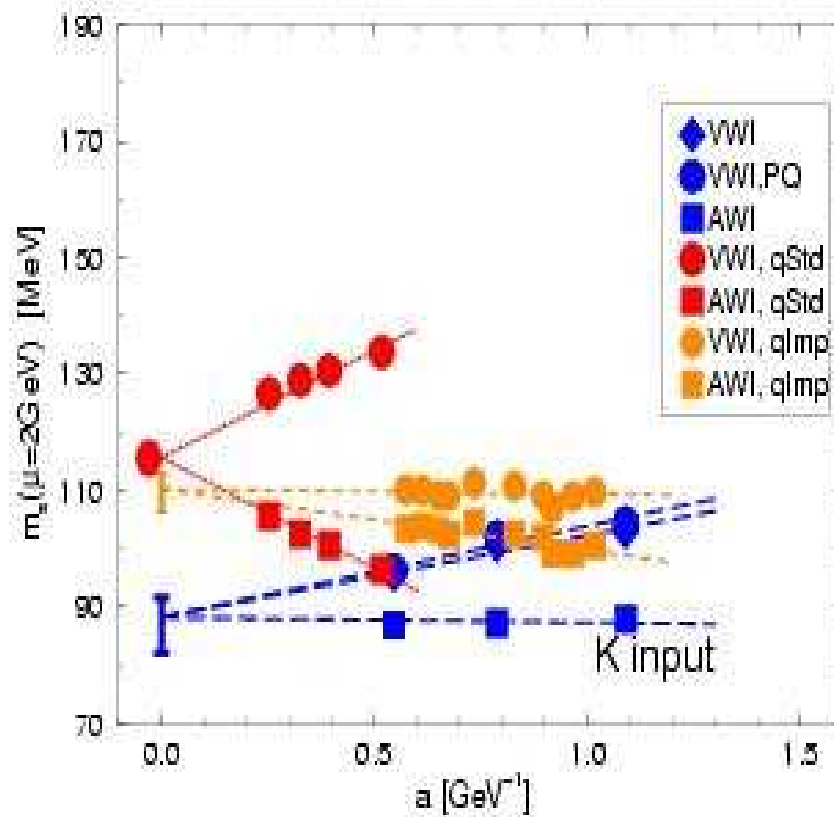
Motivation

- Previous CP-PACS spectrum studies
 - Quenched QCD (plaquette gauge + Wilson quark)
 - Nf=2 full QCD (Iwasaki RG gauge + Clover tp Csw)
additional quenched simulation with the same action combination
 - Continuum limit of spectrum and quark masses
- Two key observations
 - spectrum
 - quark mass

- ✓ O(10%) systematic deviation of the quenched spectrum from experiment is significantly reduced by dynamical u,d quarks



- ✓ Uncertainty of the strange quark mass, depending on inputs in quenched QCD, is reduced in $N_f=2$ QCD. Strange quark mass in $N_f=2$ QCD is smaller than that in quenched QCD.



Continuum extrapolations of s-quark mass

$N_f=3$ full QCD Simulations

- ✧ study and implement PHMC algorithm
- ✧ determine C_{sw} non-perturbatively
- ✧ apply the project to ESC
- ✧ port and tune the PHMC program for ES

How spectrum/quark masses change if we include dynamical s-quarks

Generating configurations with no quenching effect for studies of other physics (heavy quark system)

Action and Simulation Parameters

- Action :
 - Iwasaki RG Gauge action
 - Clover quark action C_{sw} determined non-perturbatively
- Three lattice spacings
 - $a=0.122$ fm $\beta=1.83$
 - $a=0.10$ fm $\beta=1.90$
 - $a=0.07$ fm $\beta=2.05$

at regular intervals in a^{**2}

Simulation Parameters (Cont.)

- Quark Masses

degenerate u,d quark $5 K_{ud}$ ($/ = 0.78 - 0.62$) (HMC)

s quark with different quark mass $2 K_s$ ($/ \sim 0.7$) (PHMC)

10 combinations of (K_{ud}, K_s)

valence quark $K_{val,1/2} = K_{ud} / K_s$

$\Delta\tau, N_{poly}$ are tuned in a way that

$$P_{HMC} \approx 85\%, P_{GMP} \approx 95\%$$

Simulation Parameters (Cont.)

- Lattice Size

2 fm in physical unit

meson spectrum and quark masses

a=0.122 fm 16**3x32 6000-9000 traj. (almost finished)

a=0.10 fm 20**3x40 5000-8000 traj. (already finished)

a=0.07 fm 28**3x56 1000 traj 3000 traj. (in 1-1.5 years)

continuum extrapolation using two coarse lattices

Chiral Extrapolations

- Quadratic polynomial functions in quark masses

SU(3) symmetry in dynamical masses m_u, m_d, m_s
 exchange symmetry of $m_{val,1}, m_{val,2}$

$$\begin{aligned}
 & m_V(m_{ud}, m_s; m_{val,1}, m_{val,2}) \\
 = & A^V \\
 & + B_S^V(2m_{ud} + m_s) \\
 & + B_V^V(m_{val,1} + m_{val,2}) \\
 & + D_{SV}^V(2m_{ud} + m_s) \\
 & \quad \times (m_{val,1} + m_{val,2}) \\
 & + C_{S1}^V(2m_{ud}^2 + m_s^2) \\
 & + C_{S2}^V(m_{ud} + 2m_{ud}m_s) \\
 & + C_{V1}^V(m_{val,1}^2 + m_{val,2}^2) \\
 & + C_{V2}^V m_{val,1} m_{val,2}
 \end{aligned}$$

Light-Light (LL), Light-Strange (LS),
 Strange-Strange (SS) masses are fitted
 simultaneously, ignoring correlation
 among them

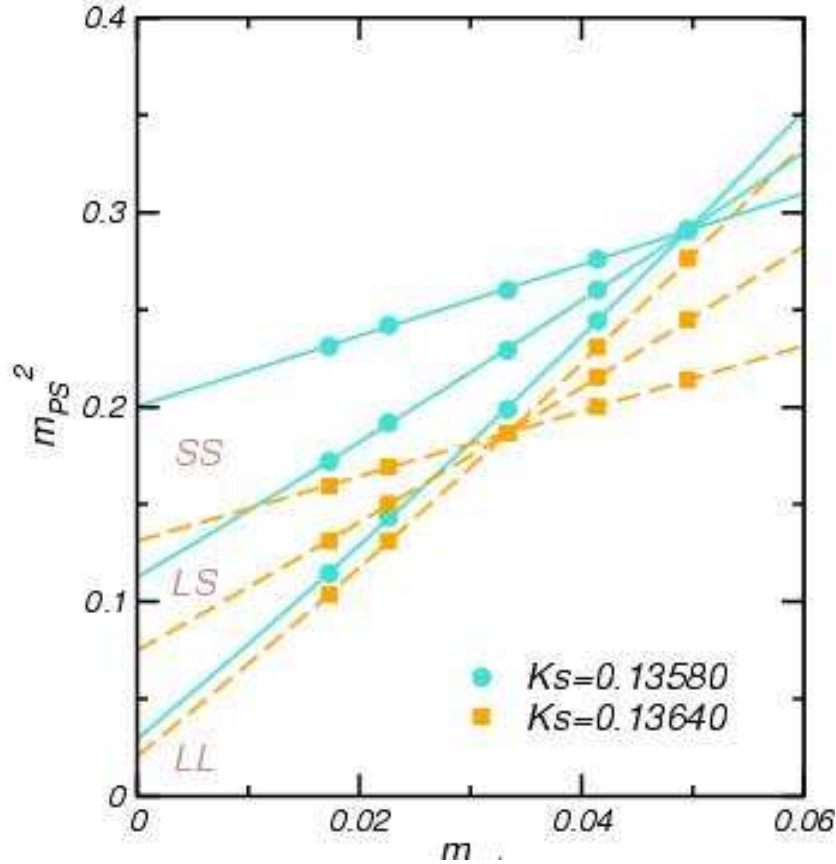
Light: $K_{val} = K_{ud}$

Strange: $K_{val} = K_s$

26 data points 8 param.

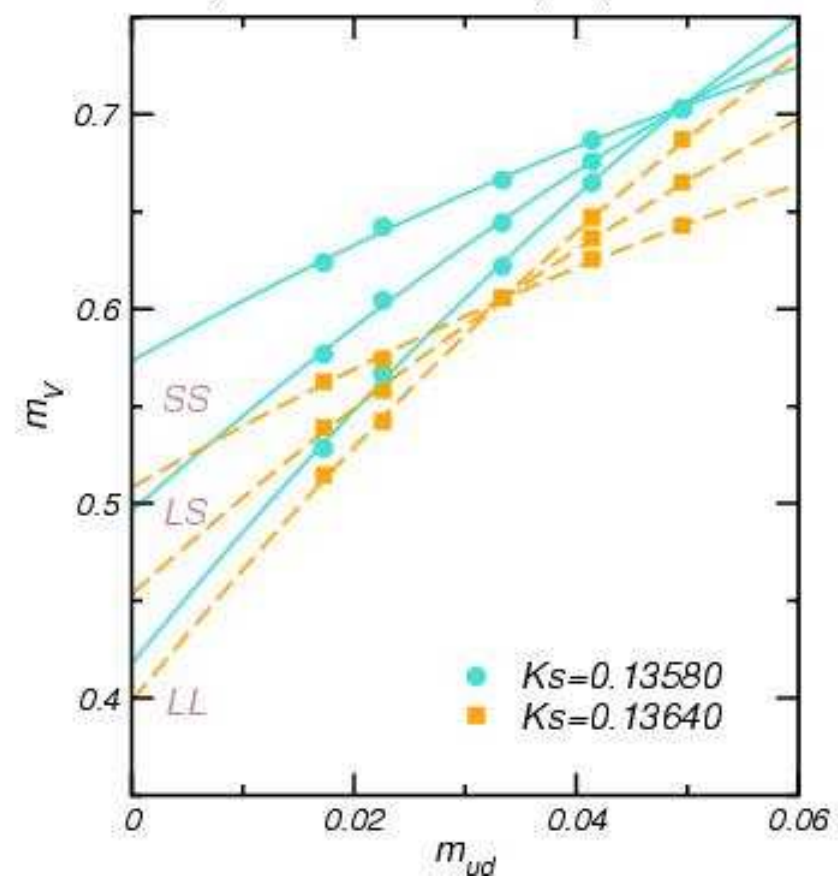
$$\chi^2 / dof = 1.09$$

$\beta=1.90, L^3 \times T=20^3 \times 40$, up to quadratic



$$\chi^2 / dof = 0.93$$

$\beta=1.90, L^3 \times T=20^3 \times 40$, up to quadratic



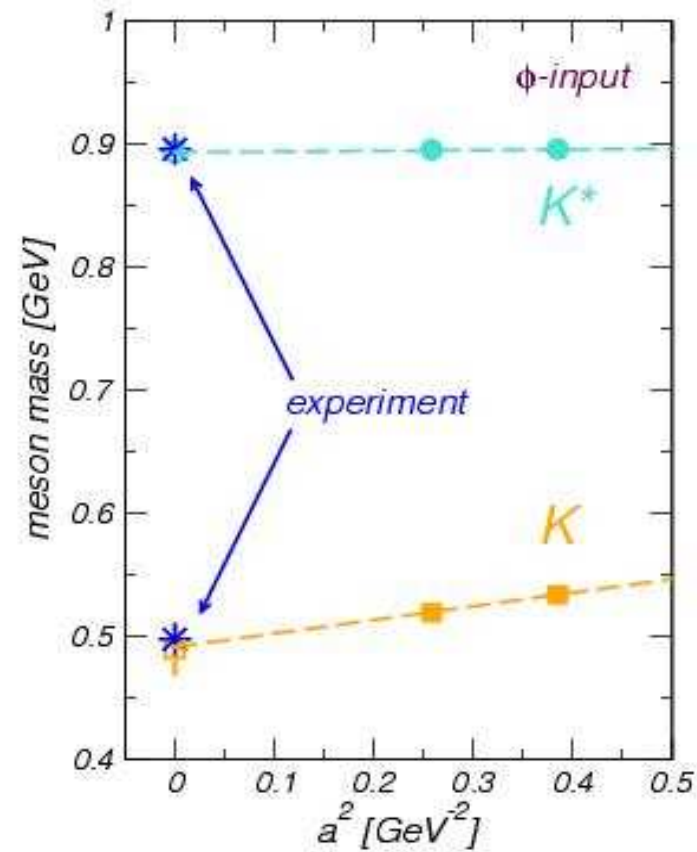
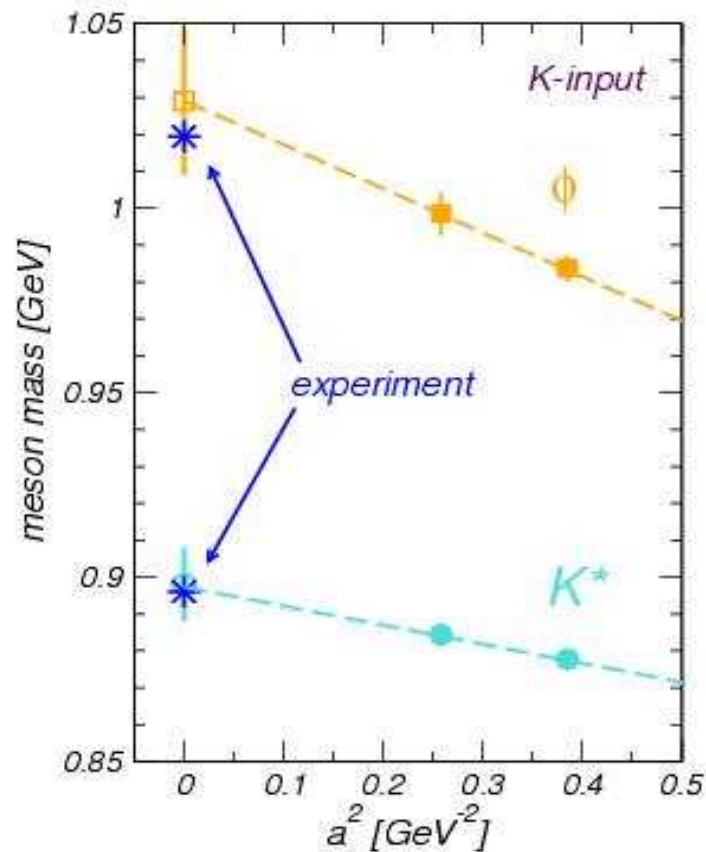
Our chiral fit functions reproduce
data well with reasonable values of

$$\chi^2 / dof$$

Spectrum

fix lattice spacing and quark masses

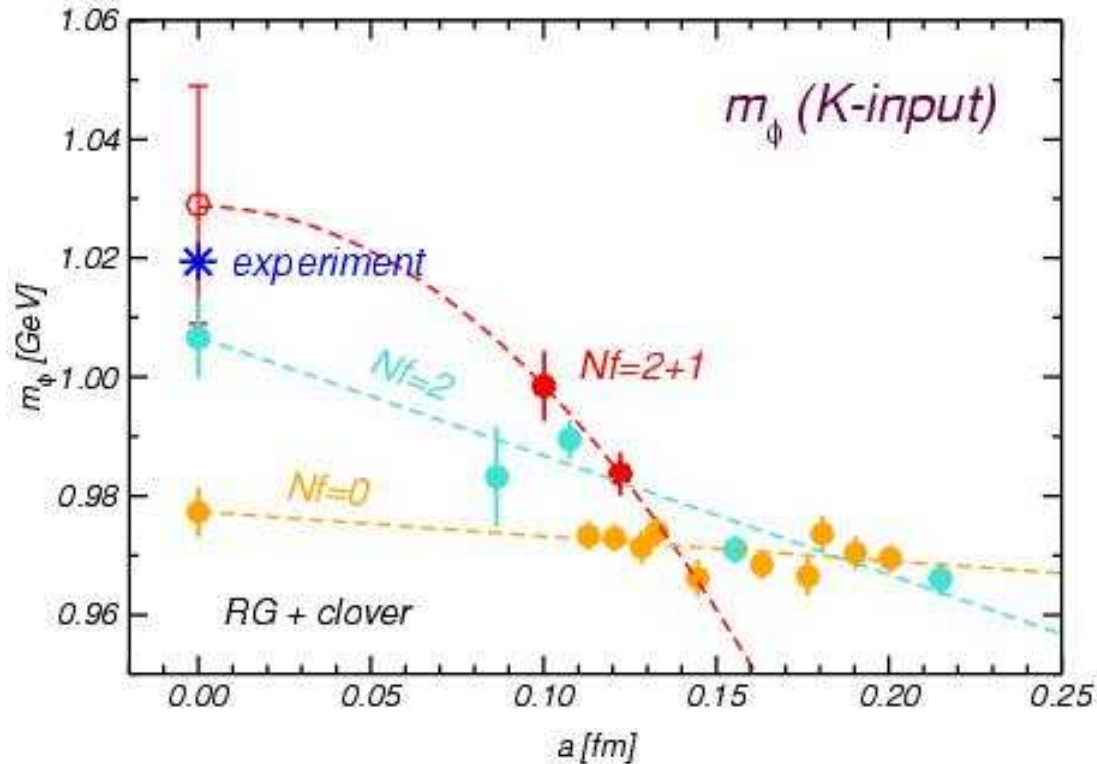
(m_π, m_ρ, m_K) K-input (m_π, m_ρ, m_ϕ) ϕ -input



$$m_h = m_0 + ca^2$$

Meson masses extrapolate to experimental values

Comparison with Nf=0 and 2



Magnitude of scaling violation (impression)

Csw (tp) for Nf=0,2

Csw (NP) for Nf=3

larger for larger #flavors ?
for $a=0.1-0.2$ fm

Current error in the continuum limit for Nf=3 is 4 times larger than that we achieved for Nf=2

We plan to reduce the error to establish dynamical s-quark effect in the spectrum

Quark Masses

Determined by two methods

$$\partial_{\mu} A_{\mu} = 2m_q^{AWI} P$$

$$2m_q^{VWI} = (1/K - 1/K_c)$$

c_A Z-factors:

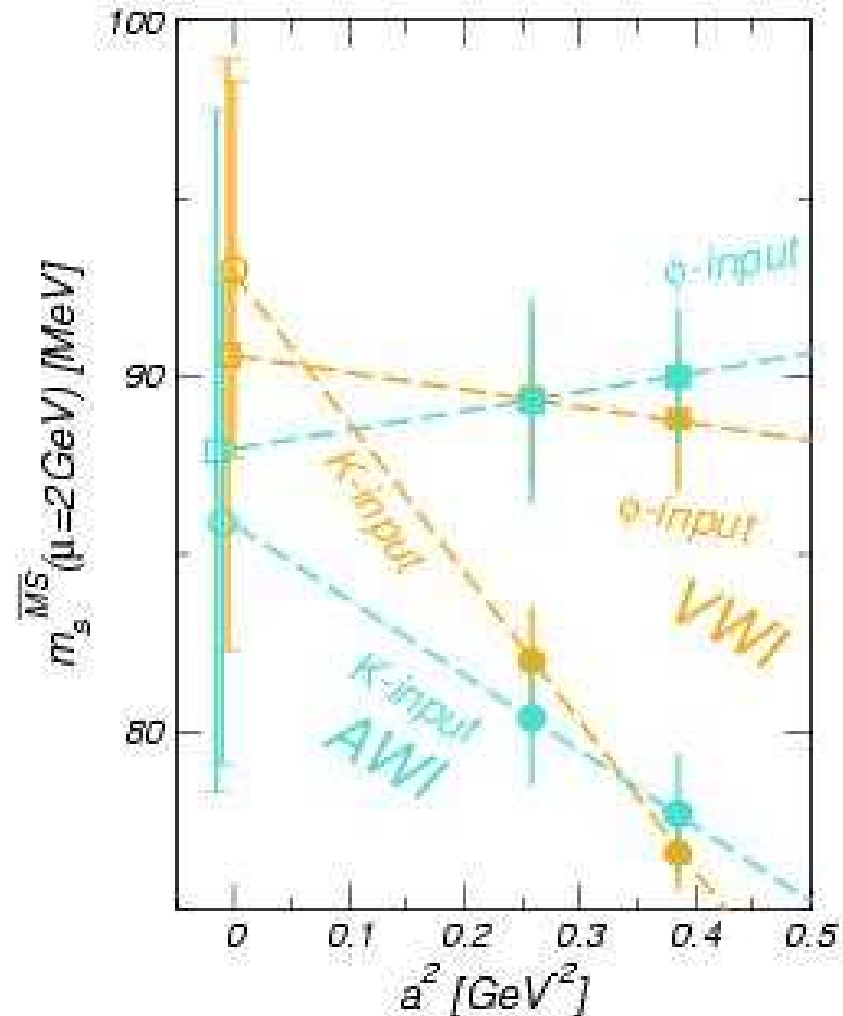
tp-improved 1-loop perturbation

Matching with \overline{MS} scheme at

$\mu = 1/a$ evolved to

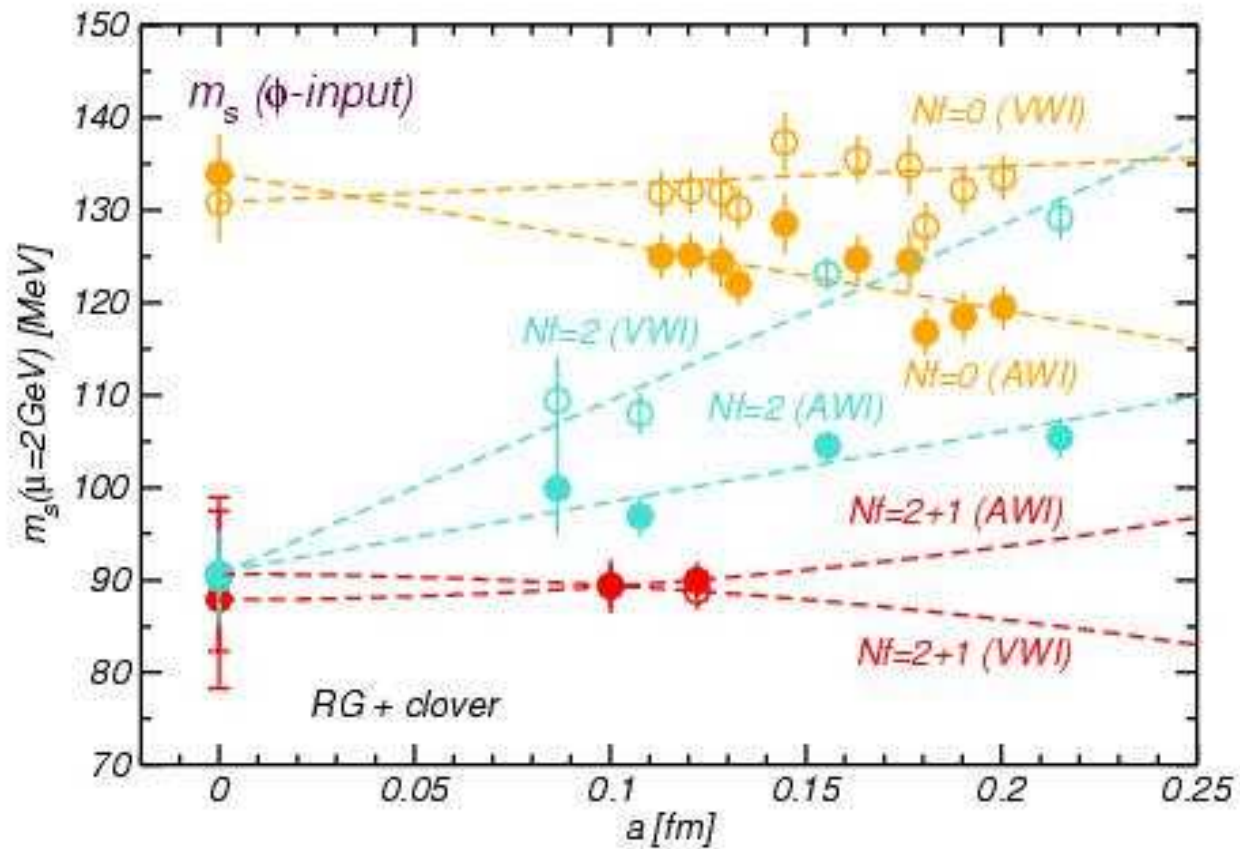
$\mu = 2\text{GeV}$

4-loop perturbation theory



Though error in the continuum limit is still large,

$$m_s^{AWI} = m_s^{VWI} \quad m_s(K) = m_s(\phi)$$

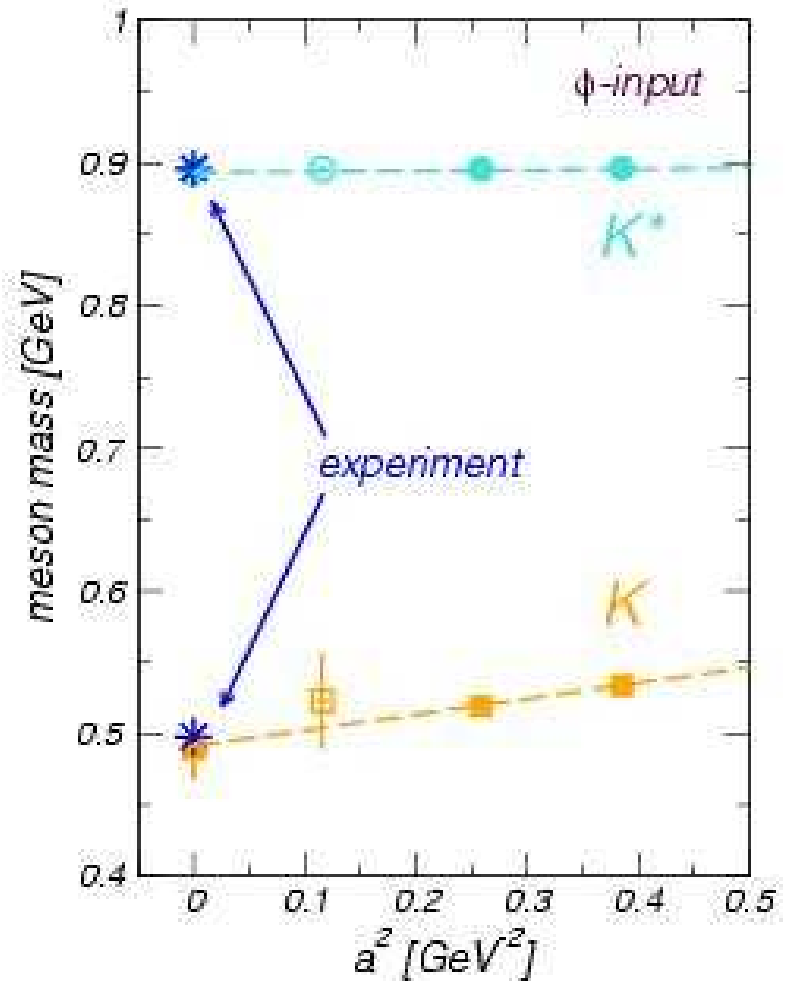


$m_s(N_f = 3) \approx m_s(N_s = 2)$ within large statistical error

Reduce the error to establish dynamical s-quark effect

Summary and Future Works

- Results of the spectrum and quark masses are very promising
 - control systematic errors from continuum extrapolations
 - reduce them with data at $a=0.07\text{fm}$



- Study and control other systematic errors
 1. chiral extrapolation with ChPT, WChPT
 2. non-perturbative calculation of c_A, Z_A, Z_P
 3. finite size effects
 - 1.6 fm vs. 2.0 fm study @ $a=0.1$ fm
 - at most 1-2% error in $L a=2$ fm
- Study and implementation of algorithms recently proposed (Hasenbush, SAP) in progress