

The Structure of the Vacuum and Conformal Properties in High Temperature QCD

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In Collaboration with

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Plan of Talk

Introduction

Phase structure; existence of conformal region

Conformal theory with an IR cutoff

Structure of the vacuum; twisted $Z(3)$ vacuum

Scaling relation of effective masses

Continuum limit and thermodynamical limit at small g

non-perturbative effects at larger g

Implications for physics

A fundamental issue at high temperature QCD

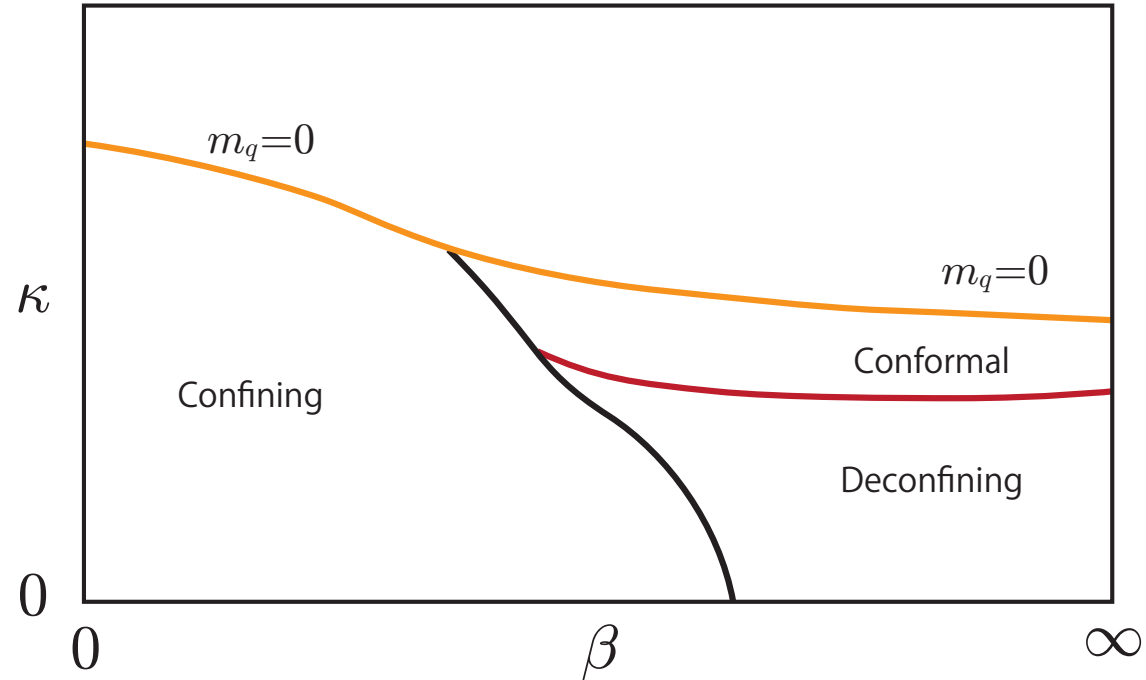
what kind of state the gluons and quarks take
at high temperatures ?

Our claim: Existence of Conformal Region

$$N_f \leq 6$$

$$m_q \leq \Lambda_{IR}$$

IR cutoff



the vacuum is a $Z(3)$ twisted vacuum modified by non-perturbative effects

PS propagators behave at large t with modified Yukawa- type decay form instead of exponential decay form.

Stage and Tools

SU(3) gauge theories with $N_f=2$ in the fundamental representation

Action: the RG gauge action and Wilson fermion action

Lattice size: $32^3 \times 16$

Aspect ratio $r = L/L_t = N/N_t = 2$

Boundary conditions: periodic boundary conditions

an anti-periodic boundary conditions (t direction) for fermions

Algorithm: Blocked HMC

Statistics: 1,000 +1,000 ~ 4000 trajectories

Computers: U. Tsukuba: CCS HAPACS; KEK: HITAC 16000

Continuum limit

Define gauge theories as the continuum limit of lattice gauge theories

$$N_x = N_y = N_z = N \quad N = r N_t \quad (\text{r aspect ratio}) \quad r = 2 \text{ in this work}$$

take the limit $a \rightarrow 0$ and $N \rightarrow \text{infinity}$

with $L = aN$ and $L_t = aN_t$ fixed

when L and/or L_t finite \Rightarrow IR cutoff

Conformal theories:

IR cutoff: an indispensable ingredient

in contrast with QCD

Thermodynamical Limit

$$L \rightarrow \infty$$

Keeping $T = 1/(N_t a)$ constant

Conformal theory with an IR cutoff

PRD87, 89

A running coupling constant

$$g(\mu; T)$$

the IR fixed point

$$g^*\left(\frac{1}{N_T T}; T\right)$$

IR cutoff T

RG argument

$$m_q \leq \Lambda_{IR} \quad \text{Conformal region}$$

RG scaling relation

Extension of the scaling relation

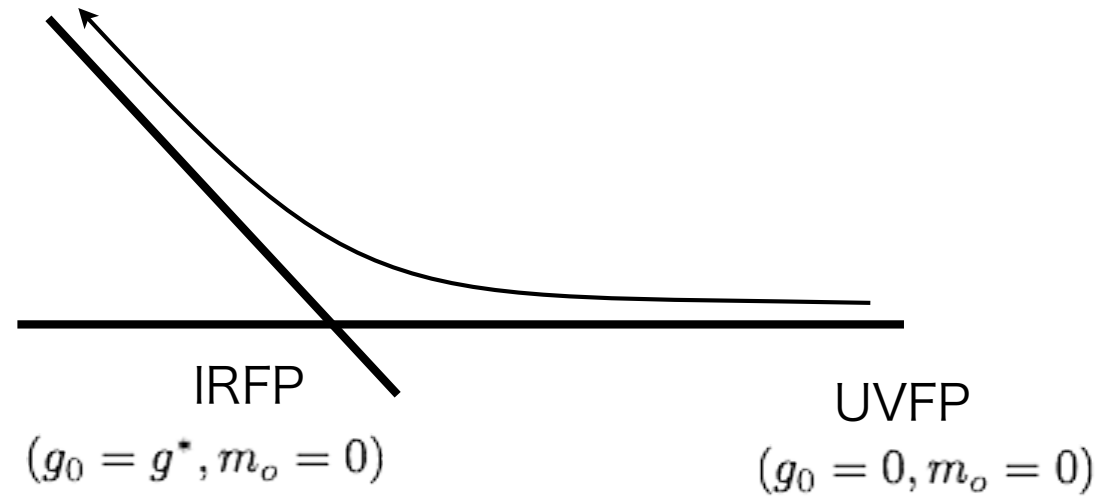
PLB



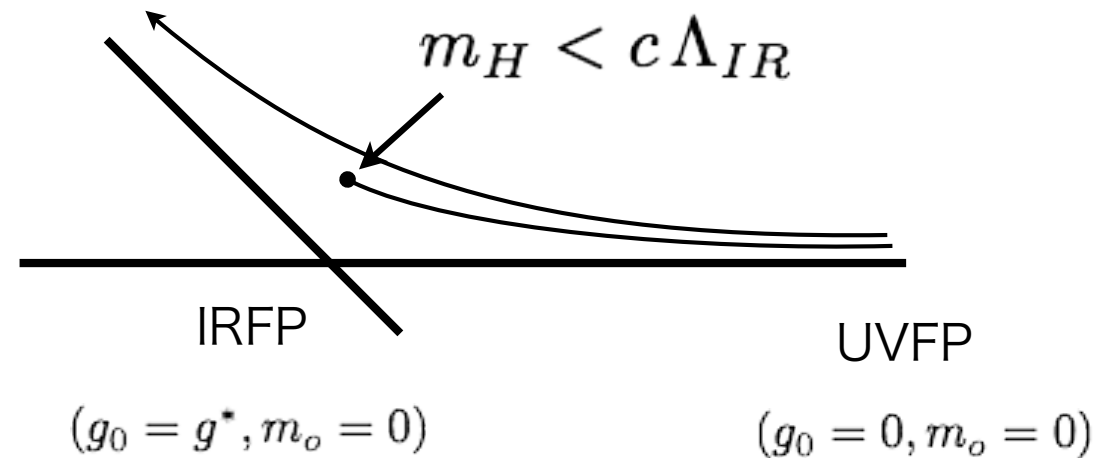
the IR fixed point

RG argument

When $\Lambda_{IR} = 0$



When $\Lambda_{IR} = \text{finite}$



Z(3) Symmetry

satisfied at $g=0$; broken at $g > 0$

one-loop calculation in term of Polyakov loops in spacial directions
on a finite lattice

$$U_i = \text{diag}(e^{i2\pi a_i}, e^{i2\pi b_i}, e^{i2\pi c_i})$$

$m_q=0.0$: The lowest energy state \sim $\exp(\pm i2/3\pi)$ $\exp(\pm i2/3\pi)$ $\exp(\pm i2/3\pi)$

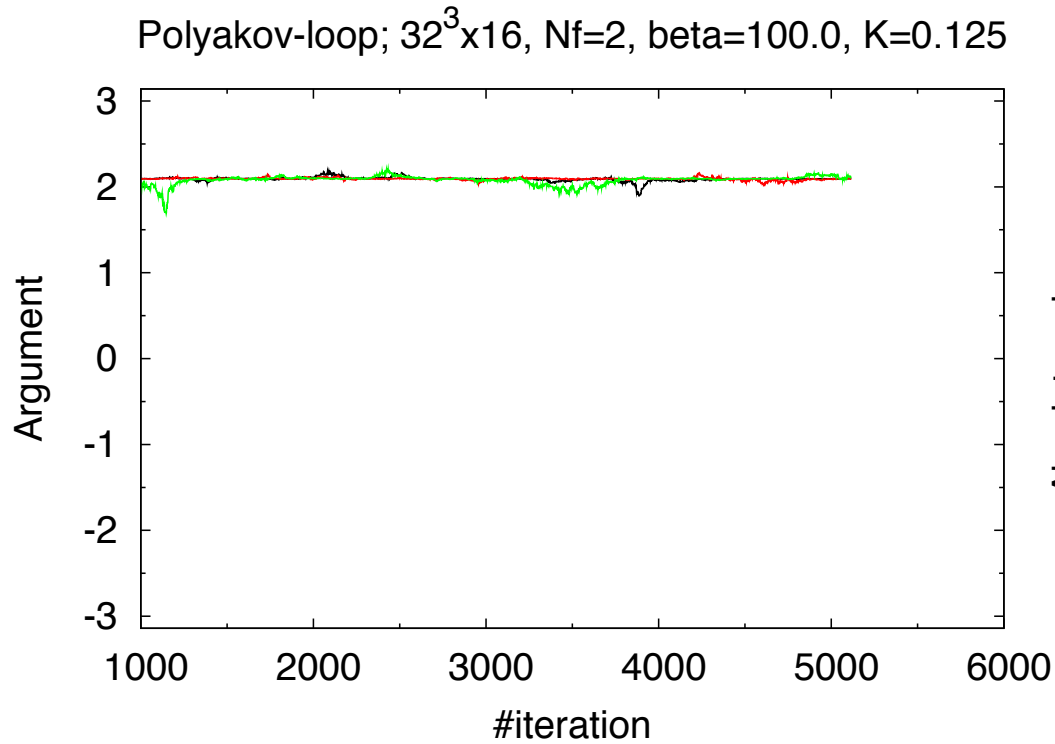
The second lowest energy state \sim $\exp(\pm i2/3\pi)$ $\exp(\pm i2/3\pi)$ 1

The third lowest energy state \sim $\exp(\pm i2/3\pi)$ 1 1

unstable state \sim 1 1 1

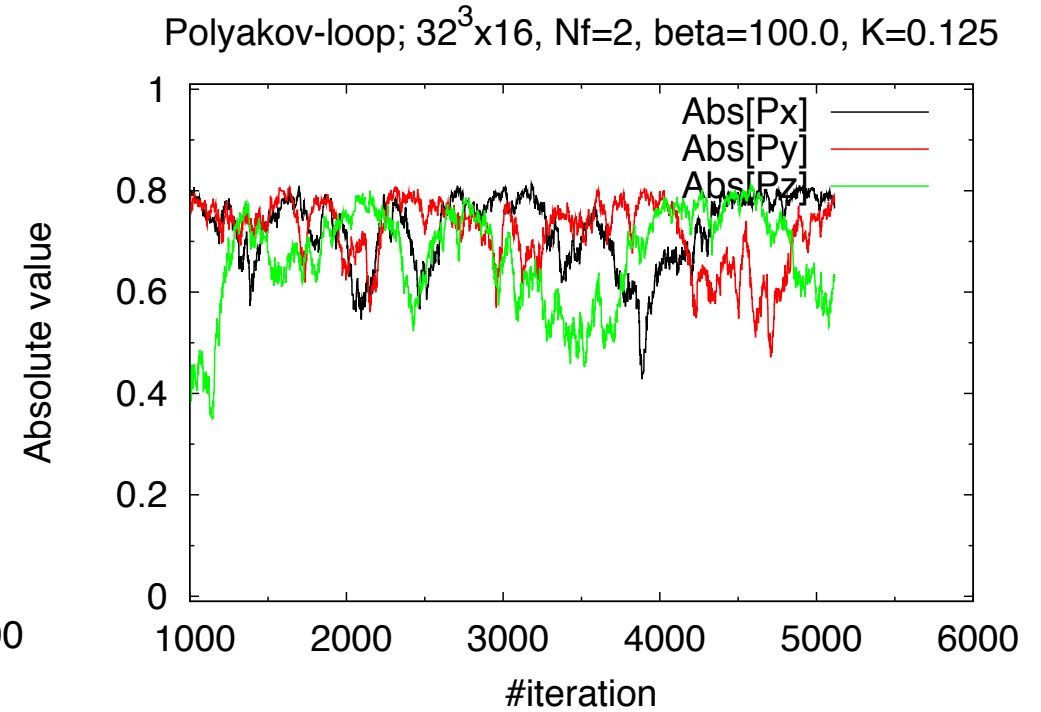
$m_q > 1.0$ stable state \sim 1 1 1

polyakov loops; beta=100.0, K=0.125



$$2\pi/3 = 2.09$$

Z(3) twisted vacuum



magnitude ~ 0.8

modified by non-perturbative effects

Scaled effective masses of PS propagators

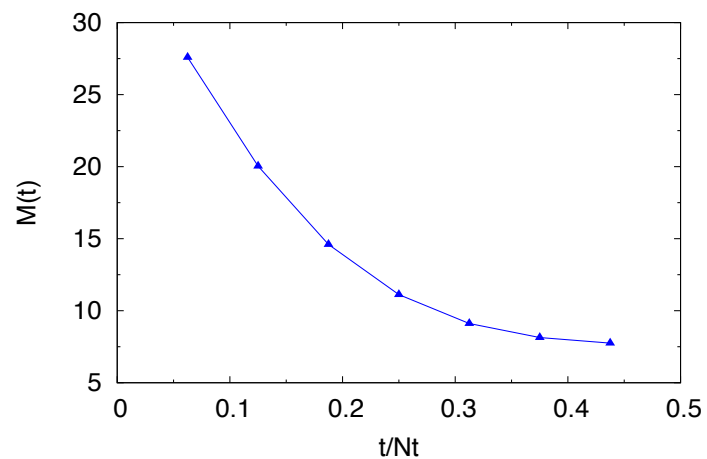
$$m(\tau, N, N_t) = N_t M(\tau, N, N_t) \quad \tau = t/N_t$$

$$M(t) = \ln \frac{G(t)}{G(t+1)}$$

twisted vacuum

32x16

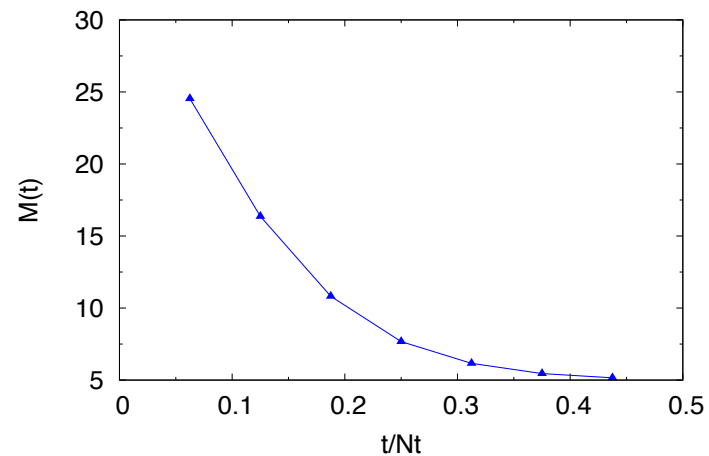
32x16;free; twisted



trivial vacuum

32x16

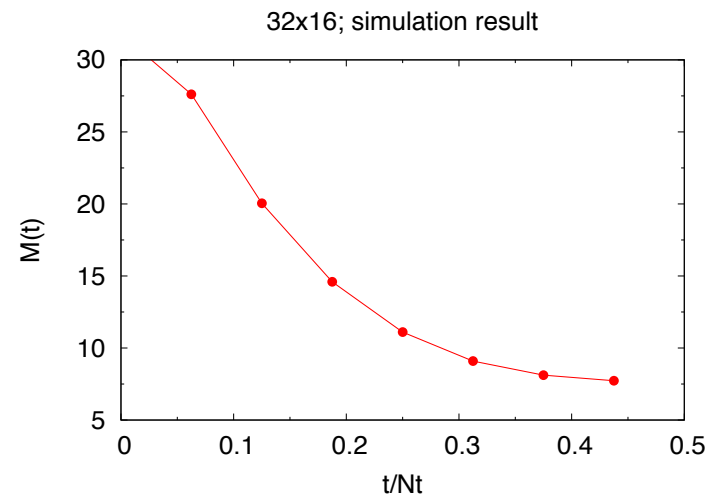
32x16;free; trivial



Scaled effective masses

simulation result
beta=100.0

32x16



Scaled effective masses

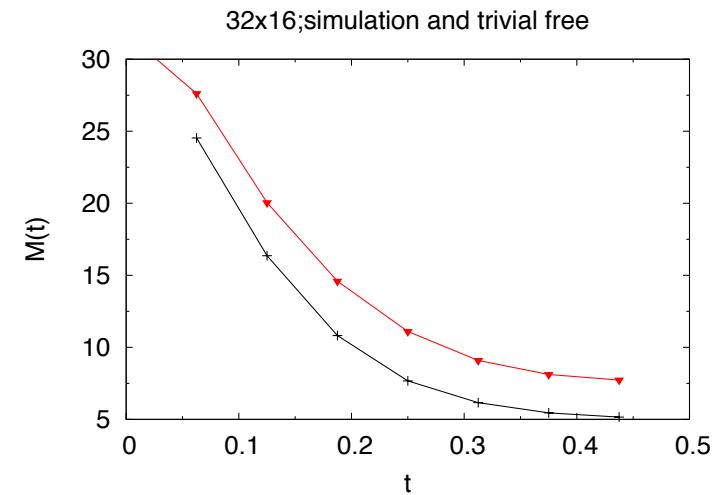
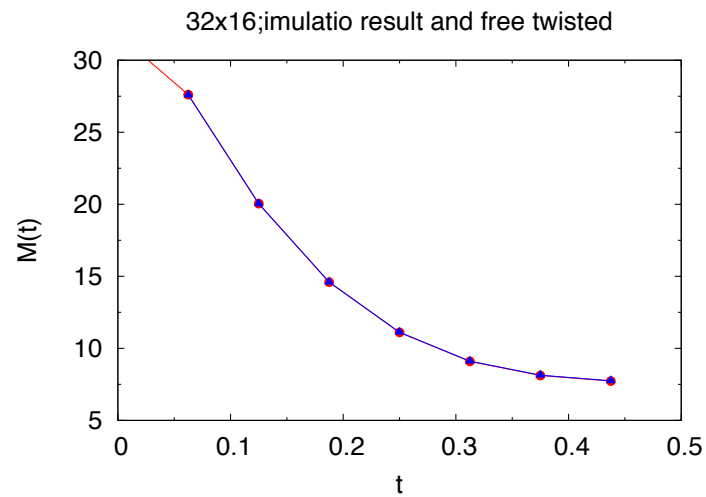
overlapped with simulation result

twisted vacuum

trivial vacuum

32x16

32x16



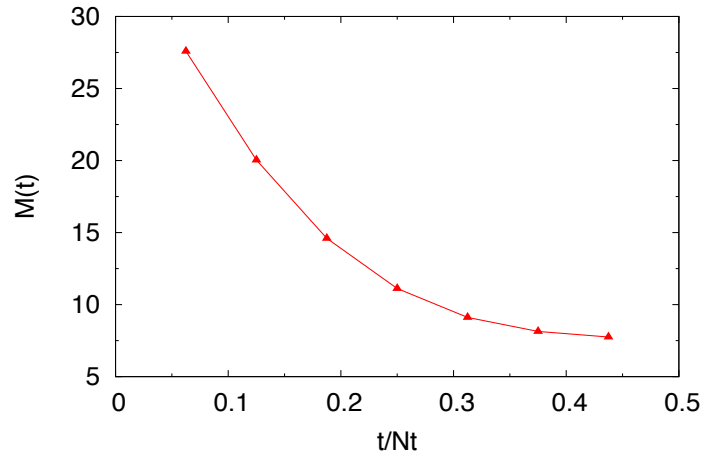
overlapped completely

Scaling law of scaled effective masses

$$m(\tau, N, N_t) = m(\tau, N', N'_t)$$

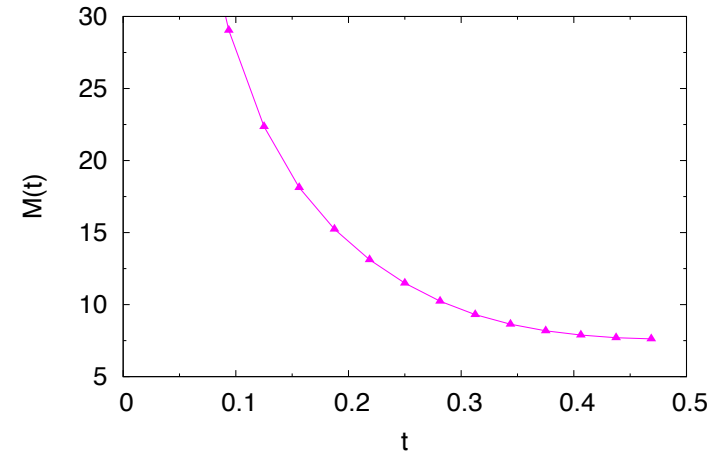
32x16

32x16;free; twisted



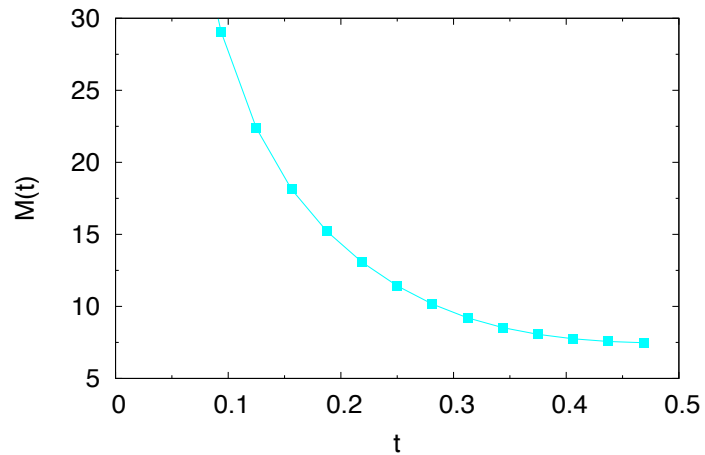
64x32

64x32;free; twisted



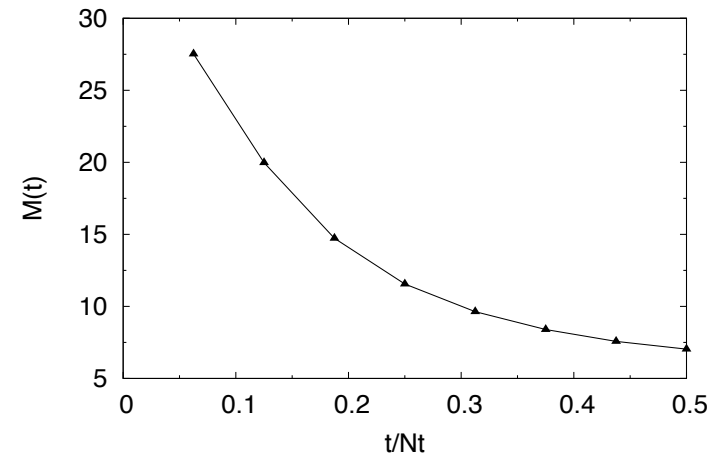
128x32

128x32;free twisted

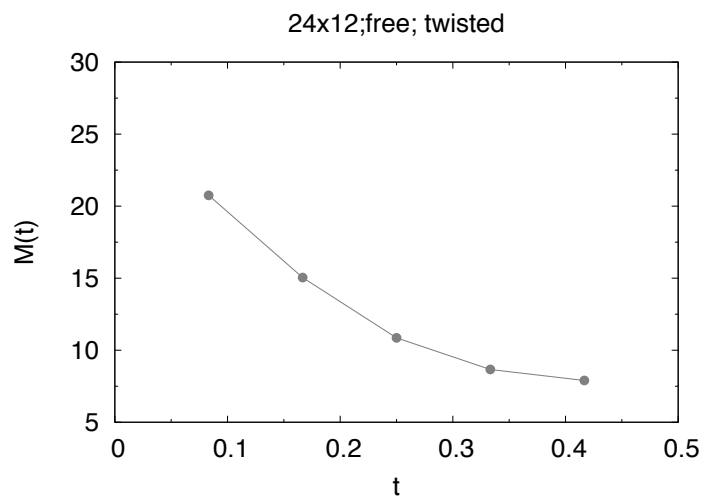


24x24

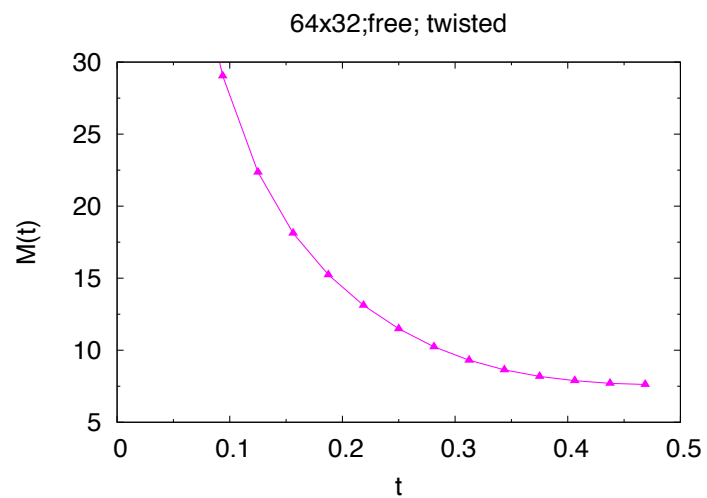
24x24;free; twisted



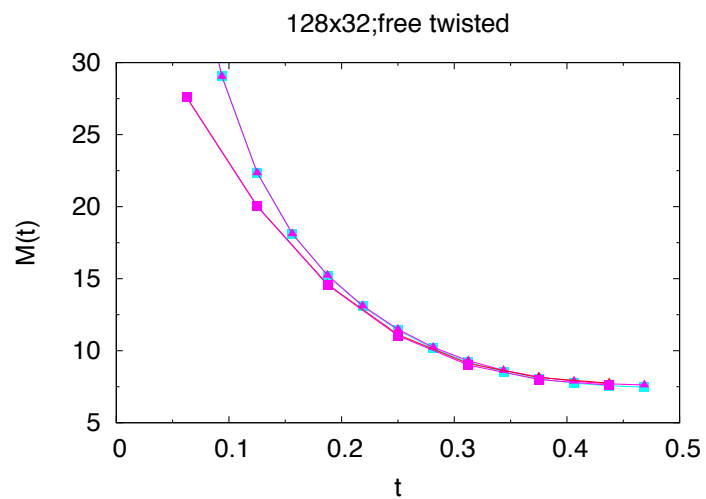
24x12



64x32



128x32; 64x32; 32x16; 64x16



Scaling law enables us to take the both limits

Continuum limit

$N \rightarrow \infty$, $Nt \rightarrow \infty$ $L = \text{const}$ $Lt = \text{constant}$ $r = N/Nt = \text{constant}$

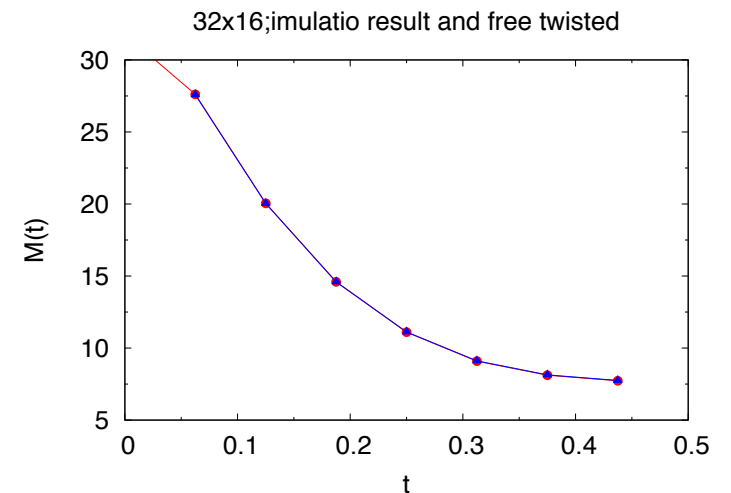
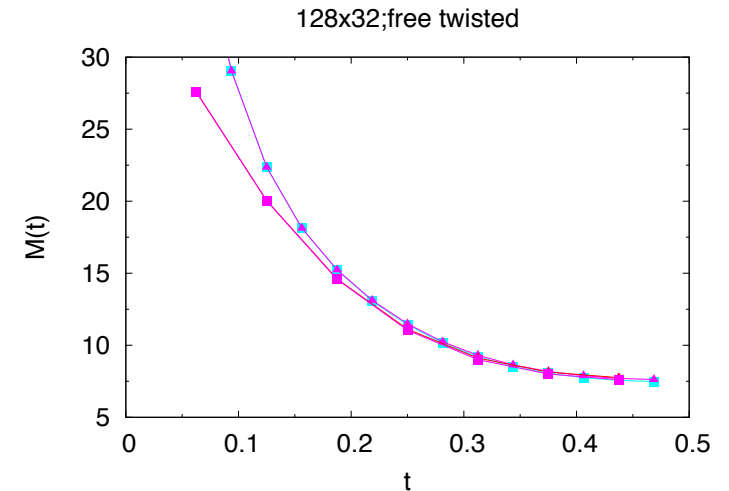
Thermodynamical limit

$L \rightarrow \infty$ with $Lt = \text{constant}$

effective mass plot is independent of T

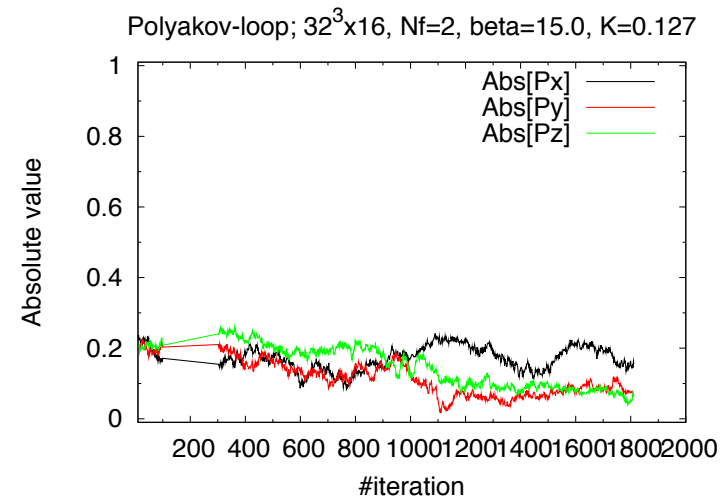
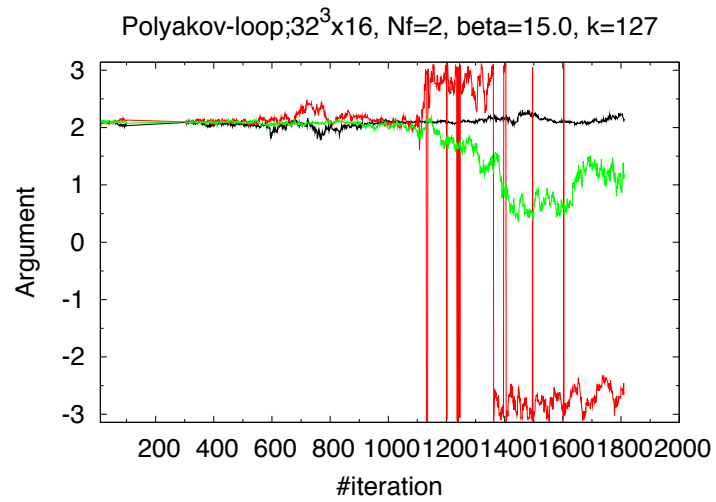
y-axis scale: temperature T

simulation result on $32^3 \times 16$ for $\tau > 0.2$
well represents the result in the continuum limit
and in the thermodynamical limit



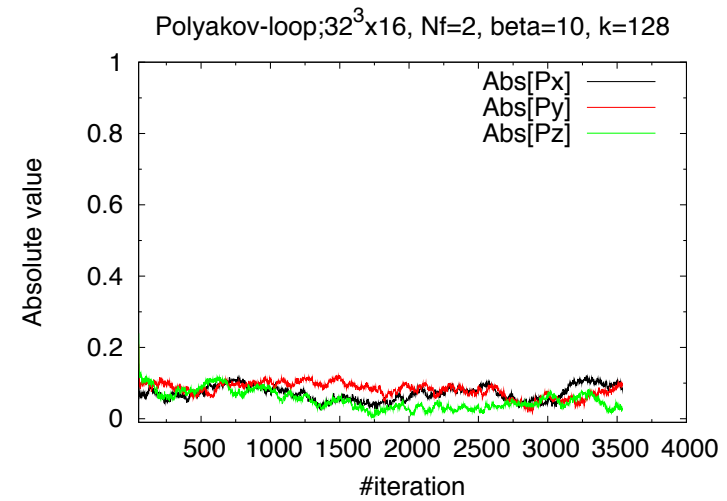
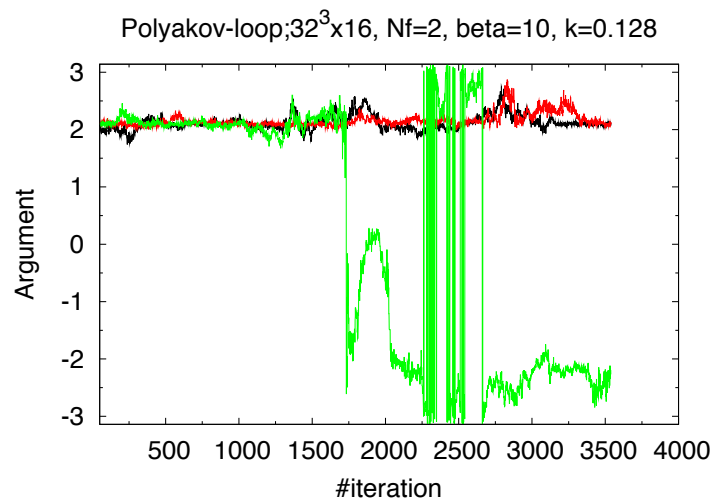
Along the massless line

beta=15.0



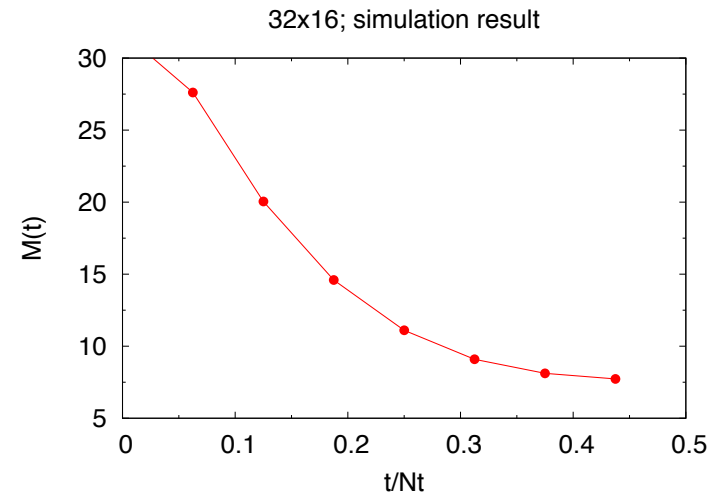
Along the massless line

beta=10.0

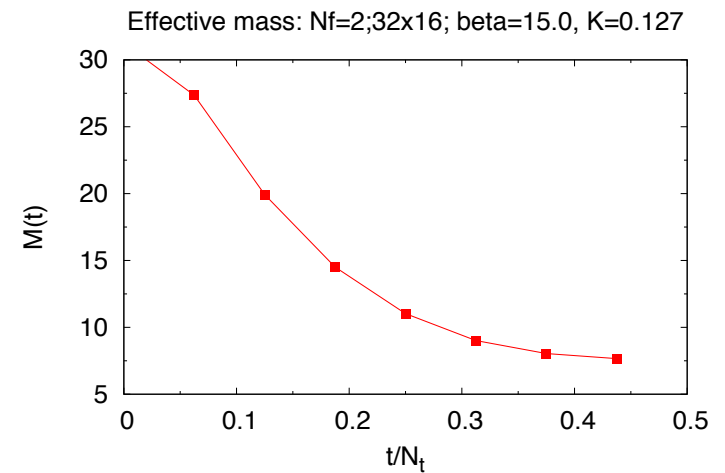


Along the massless line

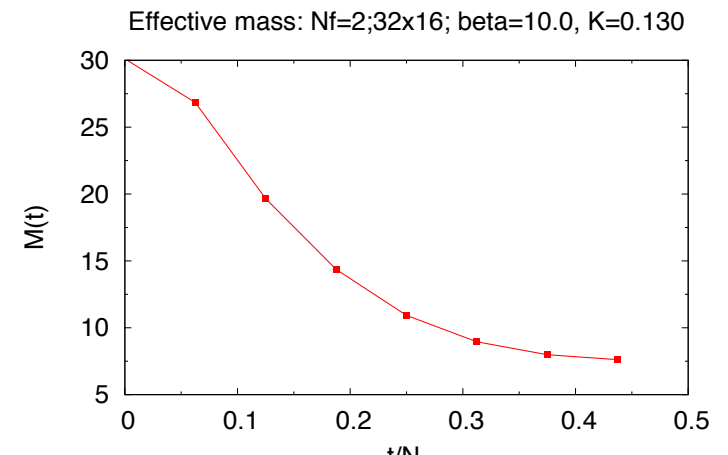
beta=100.0



beta=15.0



beta=10.0



Along the massless line

As g becomes larger non-perturbative effects larger

The $Z(3)$ twisted structure and Conformal behavior
remain

Remarks

the free massless fermion system is a typical example of conformal theory irrespective of the structure of vacuum

if the system is analytically connected with the massless fermion, it will exhibit conformal properties

Implications for physics

At very high temperature quarks and gluons are free particles not in the trivial vacuum but in the $Z(3)$ twisted one. The very **slow approach to Stefan Boltzmann ideal gas** is due to that the vacuum is not the trivial vacuum and the nonperturbative effects do not disappear even at large beta

In a conformal theory with an IR cutoff, the hyper-scaling relations is satisfied.

$m_{PS} = c m_q^{1/(1+\gamma^*)}$ with γ^* the anomalous mass dimension.

Non-analytic behavior of the m_{PS} in terms of the m_q may be a solution of the recent issue whether **the $U(1)$ symmetry** recovers at the chiral transition point for $N_f=2$

The existence and the dissociation of **quarkonia** at high temperature may be related with the conformal state and deconfining state of the quarkonia.

The transition occurs at the mass $m_{PS} \sim c T$; $c \sim 4 \pi$

Thank you very much !

金谷さん

還暦おめでとうございます

金谷さんとの邂逅

1987-90 特別推進 QCDPAX

特別配置助手 公募

ハード・ソフトバグ洗い出し 丸1年

Pure SU(3) gauge theory

並列計算機のプログラミング

細心の注意：コピー

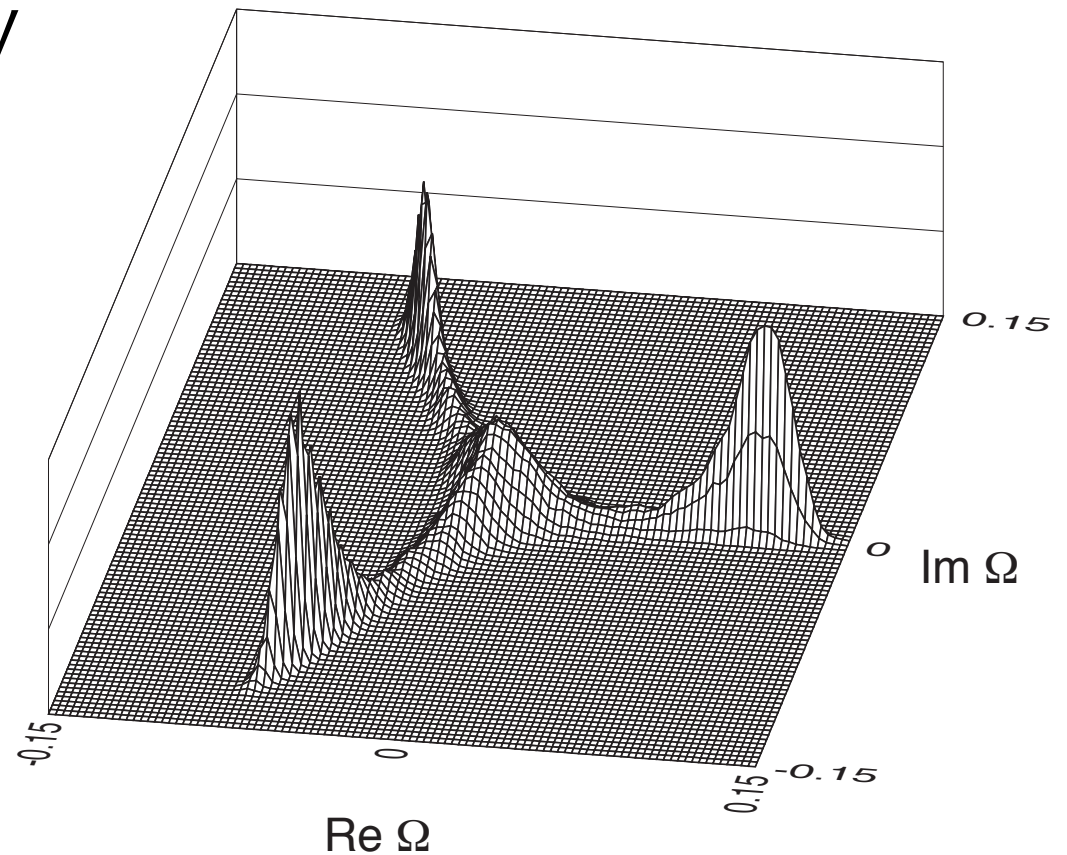
Z(3) symmetry

PRD 46 (1992) 4657

at phase transition point

3 (deconfining)+

1 (confinement)



金谷さんとの邂逅-2

QCDPAX 打ち上げ

竹園 => 並木 ボトル2本

金谷さんとの共著

total 179

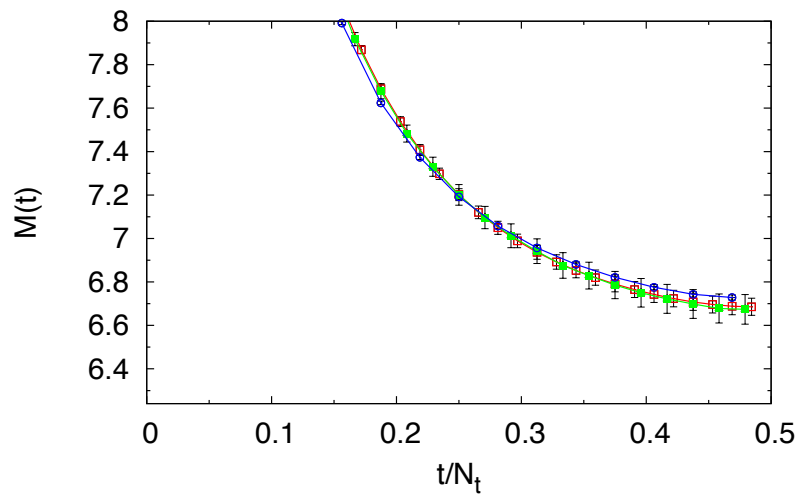
PRD 50

PRL 12

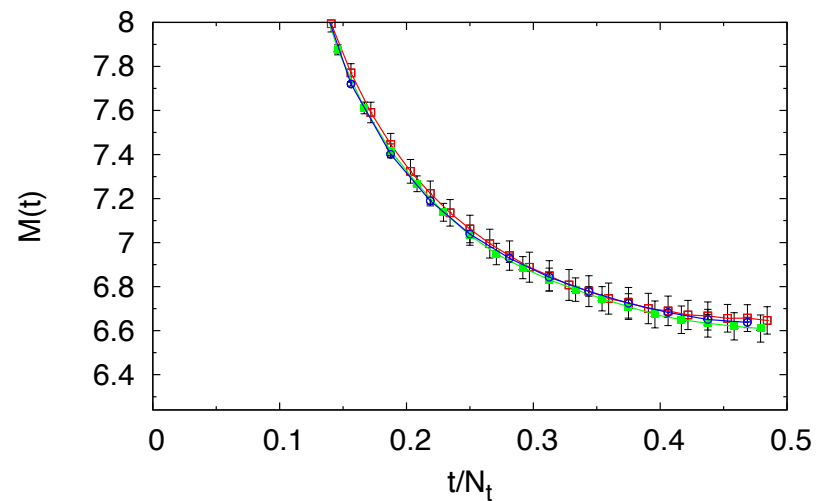
Scaling relation

$$m(\tau, N, N_t) = m(\tau, N', N'_t)$$

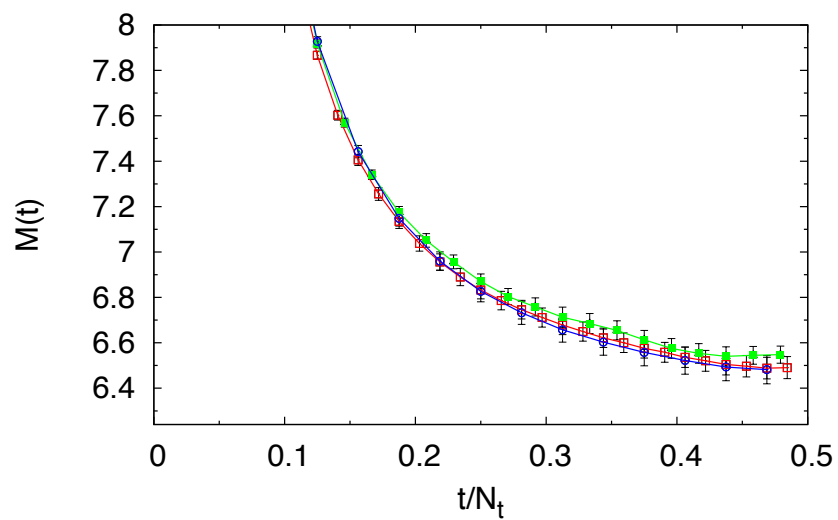
Effective mass: $N_f=16$; $\beta=10.5$, $K=0.1292$



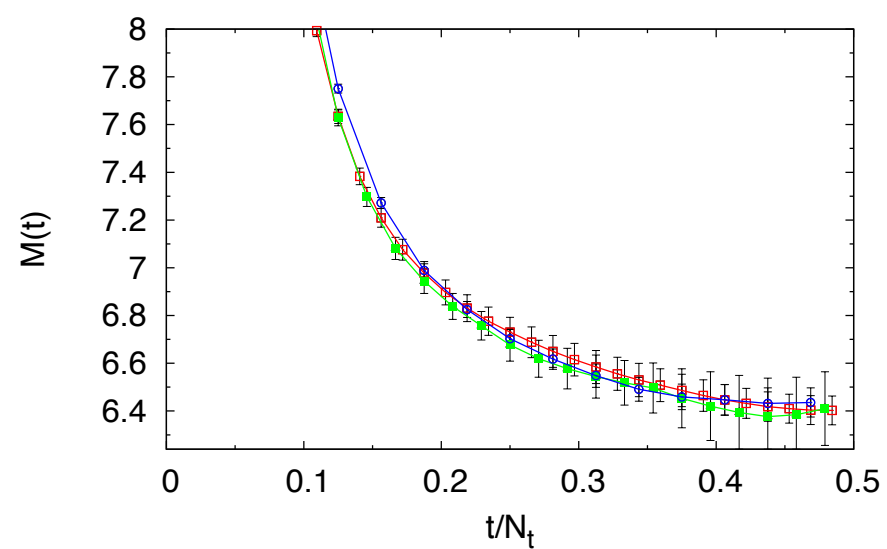
Effective mass: $N_f=12$; $\beta=3.0$, $K=0.1405$



Effective mass: $N_f=08$; $\beta=2.4$, $K=0.147$



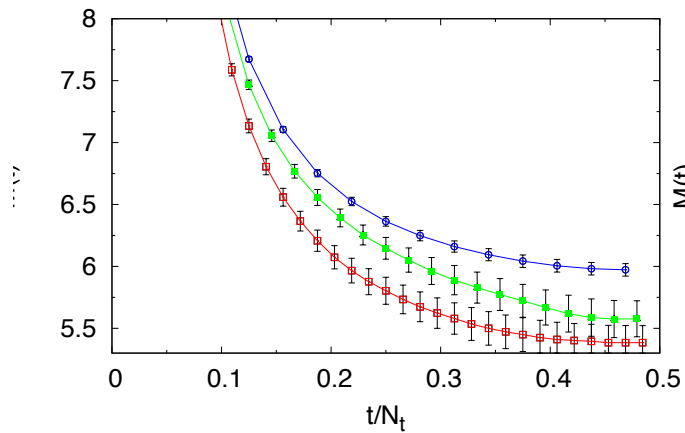
Effective mass: $N_f=07$; $\beta=2.3$, $K=0.14877$



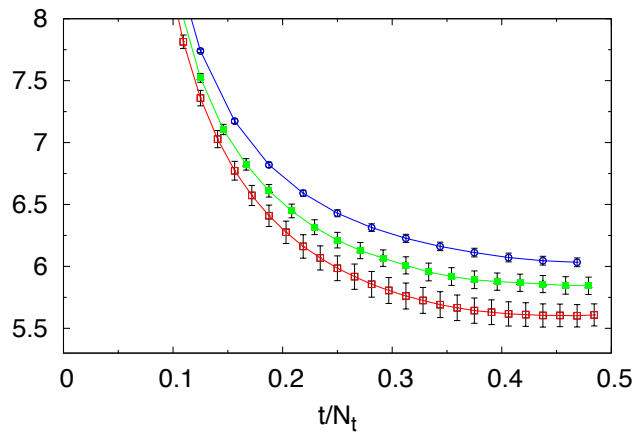
RG scaling relation

$$m(\tau, \beta, N, N_t) = m(\tau, \beta', N', N'_t)$$

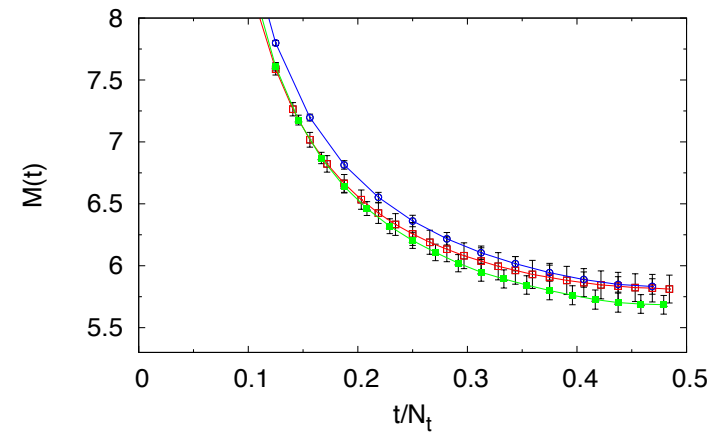
Effective mass: Nf=02; beta=6.5, K=0.147



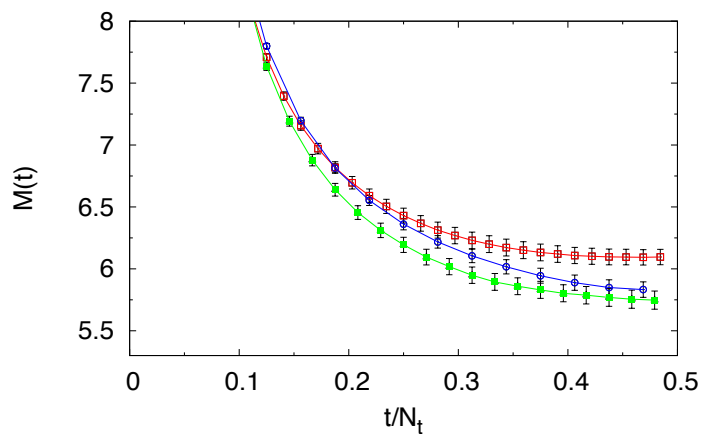
Effective mass: Nf=02; beta=6.6, K=0.147



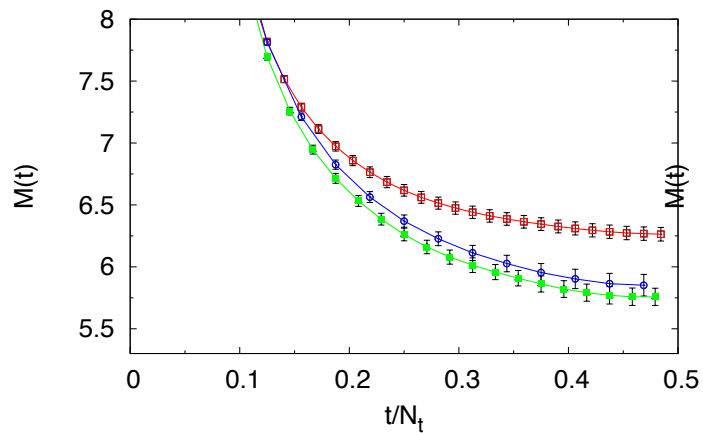
Effective mass: Nf=02; beta=6.8, K=0.1455



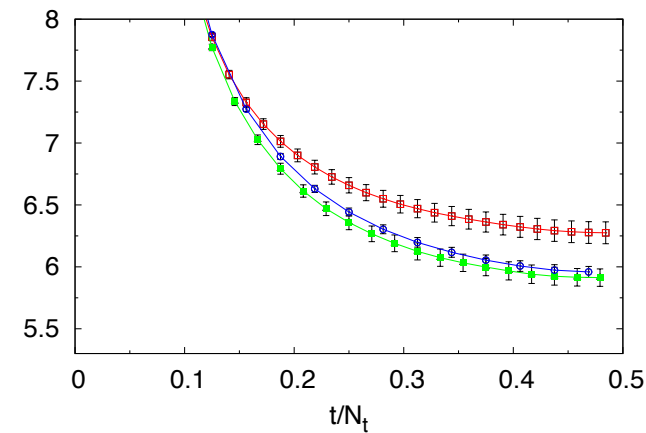
Effective mass: Nf=02; beta=6.9, K=0.146



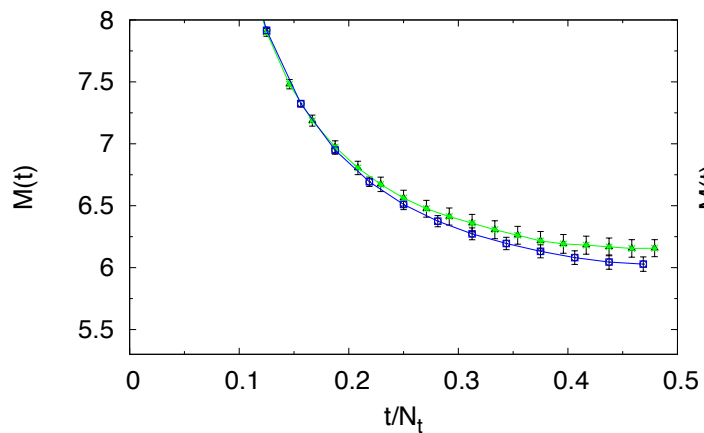
Effective mass: Nf=02; beta=7.0, K=0.144



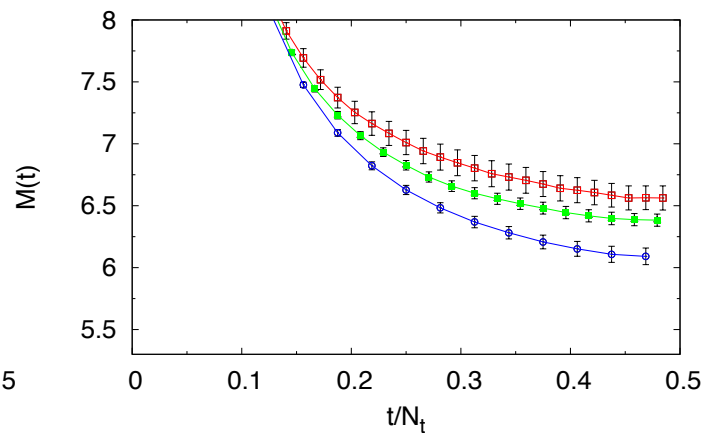
Effective mass: Nf=02; beta=7.1



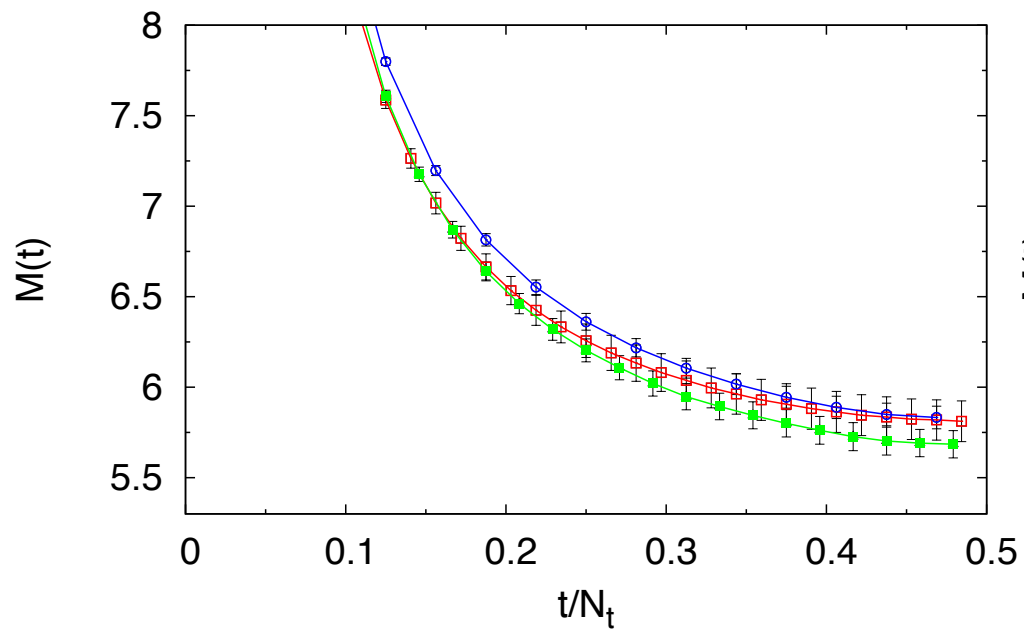
Effective mass: Nf=02; beta=7.2, K=0.143



Effective mass: Nf=02; beta=8.0, K=0.140



Effective mass: $N_f=02$; $\beta=6.8$, $K=0.1455$



$N_f=02$; $\beta=6.5(32)$, $\beta=6.7(48)$, $\beta=6.8(64)$

